ICPSR 2018

Modeling Categorical Outcomes Advanced methods of interpretation

Scott Long – β1a draft

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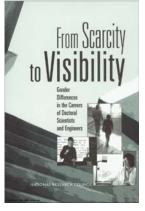
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β1a Comparing Groups



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Motivating example

Do levels of tenure differ for men and women with similar characteristics?

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Are the effects of scientific productivity on receiving tenures the same for men and women?

Readings and examples

Long & Mustillo 2018. Using predictions to compare groups in regression models for binary outcomes. See references there.

mdo18-groups-*.do

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Statistical and substantive issues

- 1. In LRM,
 - o Fit separate models for each groups
 - o Compare coefficients across groups.
- 1. Substantive concern: Academy panel did not find logit coefficients informative.
- 2. Statistical problem: Paul Allison's working paper said:

Differences in the estimated coefficients <u>tell us nothing</u> about the group differences in the effect of articles on tenure.

3. Are the logit based analyses in the NAS report wrong?

Roadmap

- 1. Linear regression model for group comparisons.
- 1. Binary regression model and scalar identification of regression coefficients
- 2. Group comparisons using predictions and marginal effects
- 3. Examples

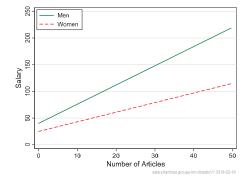
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Comparing Regressions Across Groups | 2

LRM: comparing regressions

Men: $y = \alpha^m + \beta_{articles}^m articles + \beta_{prestige}^m prestige + \varepsilon$

Women: $y = \alpha^w + \beta_{articles}^w articles + \beta_{prestige}^w prestige + \varepsilon$



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Comparing Regressions Across Groups | 3

LRM: comparing effect of articles

1. Do men and women have the same return for articles?

$$H_0: \beta_{articles}^w = \beta_{articles}^m$$

2. Test statistic standardizes the difference

$$t = \frac{\hat{\beta}_{arricles}^{w} - \hat{\beta}_{arricles}^{m}}{\sqrt{Var(\hat{\beta}_{arricles}^{w}) + Var(\hat{\beta}_{arricles}^{m}) - 2Cov(\hat{\beta}_{arricles}^{w}, \hat{\beta}_{arricles}^{m})}}$$

3. $Cov(\hat{\beta}_{articles}^{w}, \hat{\beta}_{articles}^{m}) = 0$ since the samples do not overlap

o Might not be true with complex sampling

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Comparing Regressions Across Groups | 4

LRM: Group comparing entire model

1. The hypothesis that regression planes are identical is:

$$H_0: \alpha^w = \alpha^m; \ \beta^w_{articles} = \beta^m_{articles}; \ \beta^w_{prestige} = \beta^m_{prestige}$$

If H₀ is true, it does not imply that $R_w^2 = R_m^2$.

o Indeed, I expect less explained variation for women due to discrimination.

LRM: Sources of groups differences

- 1. Groups can differ in
 - o Coefficients
 - o Unobserved heterogeneity
- 2. In LRM we can estimates coefficients and unobserved heterogeneity
- 3. In BRM we cannot estimate unobserved heterogeneity
 - o This causes an identification problem for the coefficients

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Binary regression model

1. Allow group differences in regression coefficients:

Women:
$$\Pr(y=1) = \Lambda(\alpha^w + \beta^w_{articles} articles + \beta^w_{prestige} prestige)$$

Men: $\Pr(y=1) = \Lambda(\alpha^m + \beta^m_{articles} articles + \beta^m_{prestige} prestige)$

2. We want to tests

$$H_0: \beta_{articles}^w = \beta_{articles}^m$$

3. Unfortunately, standard tests are invalid:

Because of an *identification problem*, the usual tests of this hypothesis tell us <u>nothing</u> about the underlying impact of articles for men and women (Allison 1999).

Scalar identification in the BRM

- 1. A LV approach makes this easy to see, but other approaches are possible
- 2. Regress latent y* on x:

$$y^* = \alpha + \beta x + \varepsilon$$

- 3. The mean, variance and form of ε are assumed:
- o Profit: ε is normal(0,1)
- ο Logit: ε is logistic(0, $\pi^2/3$)
- 4. The variance cannot be estimated and is assumed
 - o The values are largely a matter of convenience and tradition

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Comparing Regressions Across Groups | 6

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Computing Pr(y) from y*

1. The observed y is linked to the latent y*

$$y = \begin{cases} 1 & \text{if } y^* > 0 \\ 0 & \text{if } y^* \le 0 \end{cases}$$

2. The probability Pr(y=1|x) depends on:

- o The error distribution
- o The regression coefficients
- o The value of x where the probability is computed
- 3. Formally,

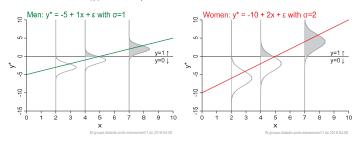
$$\Pr(y=1 \mid x) = \Pr(y^* > 0 \mid x)$$
$$= \Pr(\varepsilon < [\alpha + \beta x] \mid x)$$

4. The identification problem is illustrated in this graph

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Identification of Pr(y) but not β



- 1. β_X is <u>larger</u> for women than men.
- $2.\Delta Pr(y)/\Delta x$ is <u>identical</u> for women and men.

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Identification of βs and group comparisons

1. Regress y* on articles:

Women:
$$y^* = \alpha^w + \beta_{\text{articles}}^w$$
 articles $+ \varepsilon_m$
Men: $y^* = \alpha^m + \beta_{\text{articles}}^m$ articles $+ \varepsilon_w$

2. I want to test if articles have the same effect for men and women:

$$\beta_{\text{articles}}^{w} = \beta_{\text{articles}}^{m}$$

3. Substantively, I expect:

$$\sigma_{\rm m}^2 > \sigma_{\rm m}^2$$

4. Software traditionally assumes

Logit: $Var(\varepsilon) = \pi^2 / 3$ Probit: $Var(\varepsilon) = 1$

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Fitting probit model for each groups

1. The <u>true</u> variance of ε : $Var(\varepsilon_g) = \sigma_g$

2. Software rescales ε so that: $Var(\tilde{\varepsilon}_g) = 1 = Var(\varepsilon_g / \sigma_g)$

3. For women, the model fit by software

$$\frac{y^*}{\sigma_w} = \frac{\alpha^w}{\sigma_w} + \frac{\beta_{\text{articles}}^w}{\sigma_w} \text{ articles} + \frac{\varepsilon_w}{\sigma_w}$$
$$= \tilde{\alpha}^w + \tilde{\beta}_{\text{articles}}^w \text{ articles} + \tilde{\varepsilon}_w, \text{ where } \tilde{\sigma}_w = 1$$

4. For men

$$\frac{y^*}{\sigma_m} = \frac{\alpha^m}{\sigma_m \sigma_m} + \frac{\beta_{\text{articles}}^m}{\sigma_m} \text{ articles} + \frac{\varepsilon_m}{\sigma_m}$$
$$= \tilde{\alpha}^m + \tilde{\beta}_{\text{orticles}}^m \text{ articles} + \tilde{\varepsilon}_m, \text{ where } \tilde{\sigma}_m = 1$$

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5. I want to test:

$$H_0^{NoTilda}$$
: $\beta_{\text{articles}}^w = \beta_{\text{articles}}^m$

6. Standard software tests:

$$H_0^{Tilda} : \tilde{\beta}_{\text{articles}}^w = \tilde{\beta}_{\text{articles}}^m$$

7. The problem raised by Allison is:

o If
$$\tilde{\beta}_{\text{articles}}^{w} = \tilde{\beta}_{\text{articles}}^{m}$$
, then $\beta_{\text{articles}}^{w} = \beta_{\text{articles}}^{m}$ only if $\sigma_{m}^{2} = \sigma_{w}^{2}$.

o But, we don't know if $\sigma_{m}^{2} = \sigma_{m}^{2}$.

Allison test of the equality of true coefficients

1. If you are interested in comparing β_r^w and β_r^m

2. Assume for some variable z

$$\beta_{\tau}^{w} / \beta_{\tau}^{m} = 1$$

3. The ratio $\tilde{m{eta}}_z^w$ / $\tilde{m{eta}}_z^m$ is the relative size of $\sigma_{\!\!\!m}$ and $\sigma_{\!\!\!\!\!w}$ since:

$$\frac{\tilde{\beta}_{z}^{w}}{\tilde{\beta}_{z}^{m}} = \frac{\beta_{z}^{w} / \sigma_{w}}{\beta_{z}^{m} / \sigma_{m}} = \frac{\sigma_{m}}{\sigma_{w}}$$

4. This provides leverage to test the underlying coefficients:

$$H_0$$
: $\beta_r^w = \beta_r^m$

5. This works only if you can justify the assumption $\beta_z^w = \beta_z^m$

- o Different assumptions can lead to different results
- o There is no test of whether the assumption is correct

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Comparing effects across groups

- 1. Tests of group equality of regression coefficients are an appealing way to compare groups
- 2. Even without problems in their application, regression coefficients are not in a natural metric
 - o Are you interested in effects x on y^* or in the log(p/(1-p))?
- While odds ratios are a more natural metric, they are especially misleading in group comparisons.

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Group comparisons of odds ratios

1. ORs can be similar across groupds while DCs can be very different

Quantity	Group 0	Group 1	
$\pi(x1=1)$.026	.4	
$\pi(x1=0)$.010	.2	
DC(x1)	.016	.2	< = Groups differ
$\Omega(x1=1)$.0267	.6667	
$\Omega(x1=0)$.0101	.2500	
OR(x1)	2.64	2.67	< = Groups are similar

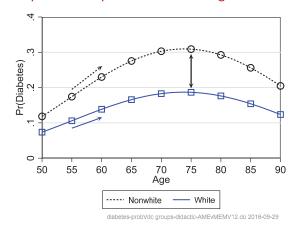
Group comparisons of marginal effects

- 1. Comparing effects on the probability have many advantages
- 2. The substantive meaning is clear
- 3. The can deal with interactions and polynomials

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Comparisons of probabilities & marginal effects



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Roadmap

- 1. We consider probabilities and DCs for two groups using logit.
- 2. Methods generalize to
 - o Any number of groups
 - o Any model that makes predictions
 - o With any measure of effect (e.g., MC, RRR)
 - o Methods are useful for LRM when there are nonlinearities

Notation

x Vector with K regressors

x* Specific values of the x's

g Group (g=1 and g=0)

 \mathbf{v}^{g} Vector of regression parameters for group g (not $\mathbf{\beta}^{g}$)

 $\pi(x, g)$ Pr_g(y=1|x) using compact notation

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Fitting a model for multiple groups

1. If $Cov(\hat{\beta}_k^0, \hat{\beta}_k^1) = 0$, you can fit separate equations for each group

Group 0: $\pi(\mathbf{x}, g = 0) = F(\mathbf{x}' \mathbf{\gamma}^0)$

Group 1: $\pi(\mathbf{x}, g = 1) = F(\mathbf{x}' \gamma^1)$

2. Or fit one equation with interactions:

$$\pi(\mathbf{x}, g) = F(\lceil g \times \mathbf{x}' \mathbf{y}^1 \rceil + \lceil (1 - g) \times \mathbf{x}' \mathbf{y}^0 \rceil)$$

so that

$$\pi(\mathbf{x}, g = 1) = F(\mathbf{x}'\mathbf{y}^1)$$
 and $\pi(\mathbf{x}, g = 0) = F(\mathbf{x}'\mathbf{y}^0)$

- 3. Joint estimations facilitates post-estimation computations and might be required with complex sampling.
- 4. A regressor can be eliminated for one group by constraining γ_k^s =0.

Comparing predictions

1. A group differences is the DC with respect to group at given values of x:

$$\frac{\Delta \pi(\mathbf{x} = \mathbf{x}^*)}{\Delta g} = \pi(\mathbf{x} = \mathbf{x}^*, g=1) - \pi(\mathbf{x} = \mathbf{x}^*, g=0)$$

2. To test if the conditional probabilities are equal:

$$H_0: \frac{\Delta \pi (\mathbf{x} = \mathbf{x}^*)}{\Delta g} = 0 \quad \text{or} \quad H_0: \pi (\mathbf{x} = \mathbf{x}^*, g = 0) = \pi (\mathbf{x} = \mathbf{x}^*, g = 1)$$

Ways to use group differences

- 1. Predictions at a single location
 - $\circ\,$ Do white men at 40 have the same probability as nonwhite men at 40?
- 2. Tables comparing groups at combinations of charcateristics
 - o Racial differences in diabetes for men and women by levels of education.
- 3. Plots for continuous variables
 - $\circ\,$ Do nonwhites and whites differ in the probability of diabetes as they age?

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Comparing marginal effects

Discrete changes

1. $DC_g(x_k)$ is the change in probability as x_k changes from start to end holding other variables at specific values:

$$\frac{\Delta \pi(\mathbf{x} = \mathbf{x}^*, g)}{\Delta x_k(start \to end)} = \pi(x_k = end, \mathbf{x} = \mathbf{x}^*, g) - \pi(x_k = start, \mathbf{x} = \mathbf{x}^*, g)$$

Comparing DC(xk) across groups

1. To test if effects are equal

$$H_0 : \frac{\Delta \pi(\mathbf{x} = \mathbf{x}^*, g = 1)}{\Delta x_k(start \rightarrow end)} = \frac{\Delta \pi(\mathbf{x} = \mathbf{x}^*, g = 0)}{\Delta x_k(start \rightarrow end)}$$

2. Equivalently, test the group difference in DC(xk)

$$H_0 \colon \frac{\Delta \pi(\mathbf{x} = \mathbf{x}^*, g = 1)}{\Delta x_k(start \to end)} - \frac{\Delta \pi(\mathbf{x} = \mathbf{x}^*, g = 0)}{\Delta x_k(start \to end)} = \frac{\Delta^2 \pi(\mathbf{x} = \mathbf{x}^*)}{\Delta x_k(start \to end)\Delta g} = 0$$

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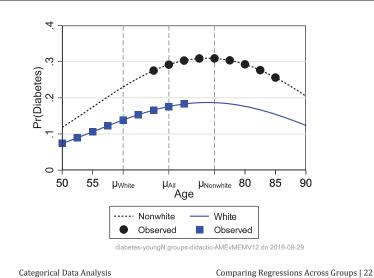
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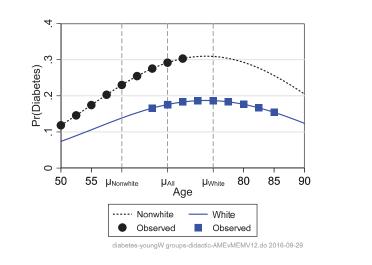
Ways to summarize the discrete change

- 1. $DC(x_k)$ depends on values of all x's where the change is estimated
 - o According, how do you summarize the effect?
- 2. Most common summary measure
 - o DCR(xk) computes the effect at representative values such as DCM
 - o ADC(x_k) averages DC($x_k | \mathbf{x}_i$) for observations in the group
- 3. DCRs and ADCs highlight different ways in which groups can differ.
 - o DCRs reflect differences in the curve at the same values of the regressors
 - o ADCs reflect differences in the curves and in the distribution of regressors.
- 4. The "best" measure is the one that answers your question.
 - o Despite some literature suggesting DCR bad, ADC good!
- 5. Consider these graphs...

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Discrete change at representative values (DCR)

1. $DCR_g(x_k | \mathbf{x} = \mathbf{x}^*)$

$$\frac{\Delta \pi(\mathbf{x} = \mathbf{x}^*, g)}{\Delta x_k(start \rightarrow end)} = \pi(x_k = end, \mathbf{x} = \mathbf{x}^*, g) - \pi(x_k = start, \mathbf{x} = \mathbf{x}^*, g)$$

2. To compare $DCR_g(x_k)$ across groups at the mean:

$$\frac{\Delta^2 \pi(\mathbf{x} - \overline{\mathbf{x}})}{\Delta x_k(\overline{x}_k \to \overline{x}_k + s_k) \Delta g} = \frac{\Delta \pi(\mathbf{x} - \overline{\mathbf{x}}, g = 1)}{\Delta x_k(\overline{x}_k \to \overline{x}_k + s_k)} - \frac{\Delta \pi(\mathbf{x} - \overline{\mathbf{x}}, g = 0)}{\Delta x_k(\overline{x}_k \to \overline{x}_k + s_k)}$$

3. If x_k is binary,

$$\frac{\Delta^2 \pi(\mathbf{x} = \mathbf{x}^*)}{\Delta x_k(0 \to 1) \Delta g} = \frac{\Delta \pi(\mathbf{x} = \mathbf{x}^*, g = 1)}{\Delta x_k(0 \to 1)} - \frac{\Delta \pi(\mathbf{x} = \mathbf{x}^*, g = 0)}{\Delta x_k(0 \to 1)}$$

- - o DCRs do not reflect group differences in the distribution of the regressors

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Average discrete change (ADC)

- 1. $ADC_g(x_k)$ averages DCs at observed x_i 's for each observation in a group.
- 2. For observation i in group q, the $DC_i(x_k)$

$$\frac{\Delta \pi(\mathbf{x} = \mathbf{x}_i, g)}{\Delta x_k(start_i \rightarrow end_i)} = \pi(x_k = end_i, \mathbf{x} = \mathbf{x}_i, g) - \pi(x_k = start_i, \mathbf{x} = \mathbf{x}_i, g)$$

3. For continuous x_k , compute ADC as x_k increases by δ from observed x_{ik} :

$$\frac{\Delta \pi(\mathbf{x} = \mathbf{x}_i, g)}{\Delta x_k(x_{ik} \to x_{ik} + \delta)} = \pi(x_k = x_{ik} + \delta, \mathbf{x} = \mathbf{x}_i, g) - \pi(x_k = x_{ik}, \mathbf{x} = \mathbf{x}_i, g)$$

4. Changes between fixed values are possible such age from 60 to 65 or a binary variable from 0 to 1.

$$\frac{\Delta \pi(\mathbf{x} = \mathbf{x}_i, g)}{\Delta x_k(start \rightarrow end)} = \pi(x_k = end, \mathbf{x} = \mathbf{x}_i, g) - \pi(x_k = start, \mathbf{x} = \mathbf{x}_i, g)$$

5. The ADC($x_k \mid g$) is the average of the DC for each observation in the group:

$$ADC_{x_k}^g = \frac{1}{N_g} \sum_{i \in g} \frac{\Delta \pi(\mathbf{x} = \mathbf{x}_i, g)}{\Delta x_k(start_i \rightarrow end_i)}$$

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Example: Racial differences in health outcomes

The literatures suggests racial differences in diabetes and health that might decline with age. Obesity and physical activity might affect racial differences in diabetes.

Data

- 1. Health and Retirement Study (HRS) of older adults in the US. In Stata, run search groupsbrm to obtain the data.
- 2. Primary variables

goodhlth Has good health? Has diabetes? diabetes white Is white? age Age

active

Is physically active? obese Is obese?

female Is female?

highschool Has high school degree?

married Is married?

ihsincome Inverse hyperbolic sine of income

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Descriptive statistics

1. Groups differ on the levels of all variables.

Variable	White (N=12,427) Std Dev	Nonwhit Mean	e (N=3,799) Std Dev	Differe ΔMean	nce P
goodhlth diabetes age active obese female	0.769 0.162 66.514 0.303 0.286 0.532	10.421 — —	0.565 0.281 64.099 0.223 0.390	9.677 — — —	0.205 -0.120 2.415 0.080 -0.104 -0.043	<.001 <.001 <.001 <.001 <.001
highschool married ihsincome	0.853 0.692 4.523	1.001	0.563 0.541 3.809	 1.164	0.289 0.150 0.714	<.001 <.001 <.001

Note: AMean is group difference in the means.

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Logit model of good health

The tests of $\beta_w = \beta_m$ are invalid as per Allison.

Logit model for good health (N =16,226).

	White			Nonwhite	•		но: въ	$v = \beta n$
Variable	1: βw	2: ORw	4: p	5: βn	6: ORn	8: p	9: F	10: p
Constant	-0.488	_	0.086	-1.541		<.001	4.71	0.034
female	0.144	1.155	0.006	-0.118	0.888	0.176	6.96	0.011
highschool	0.800	2.225	<.001	0.816	2.262	<.001	0.02	0.891
married	-0.056	0.945	0.341	-0.169	0.844	0.124	0.70	0.406
ihsincome	0.556	1.744	<.001	0.583	1.792	<.001	0.16	0.695
age	-0.018	0.982	<.001	-0.008	0.992	0.072	3.47	0.068
obese	-0.573	0.564	<.001	-0.361	0.697	0.002	3.10	0.084

Note: OR is the odds ratio; tests of H0: βw = βn are for didactic purposes.

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Logit models of diabetes

The tests of $\beta_w = \beta_m$ are invalid as per Allison.

Logit model for diabetes (N =16,226).

	White			Nonwhite	Э		H0: βw	= βn
Variable	1: βw	2: ORw	4: p	5: βn	6: ORn	8: p	9: F	10: p
Constant	-9.627		<.001	-11.169		<.001	0.40	0.529
female	-0.400	0.670	<.001	-0.079	0.924	0.427	7.27	0.009
highschool	-0.253	0.776	0.001	-0.142	0.867	0.160	0.92	0.342
married	0.070	1.073	0.333	0.064	1.066	0.548	0.00	0.960
ihsincome	-0.189	0.828	<.001	-0.131	0.877	<.001	1.61	0.210
age	0.243	1.274	<.001	0.299	1.348	<.001	0.65	0.422
agesq	-0.002	0.998	<.001	-0.002	0.998	<.001	0.78	0.382
active	-4.048	0.017	0.302	-2.557	0.078	0.678	0.04	0.849
activeXage	0.115	1.122	0.331	0.052	1.053	0.783	0.07	0.791
activeXagesq	0009	0.999	0.310	0003	1.000	0.835	0.11	0.737
obese	1.163	3.199	<.001	0.740	2.095	<.001	9.35	0.003

Note: OR is the odds ratio; tests of $H0: \beta w = \beta n$ are for didactic purposes.

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Comparing marginal effects

Comparing $ADC_g(x_k)$ for diabetes

Panel A: Average discrete change for logit model for diabetes (N=16,226).

Variable	White 1: ADC	2: p	Nonwhite 3: ADC	4: p	Differer 5: ADC	nce 6: p
female	-0.051	<0.001	-0.015	0.431	-0.036	0.089
highschool	-0.033	0.001	-0.027	0.160	-0.006	0.763
married	0.009	0.330	0.012	0.546	-0.003	0.875
ihsincome	-0.022	<0.001	-0.024	<0.001	0.002	0.779
age	0.011	<0.001	0.027	<0.001	-0.016	0.002
active	-0.053	<0.001	-0.084	<0.001	0.031	0.110
obese	0.169	<0.001	0.146	<0.001	0.022	0.408

Note: The effect of age is for a five-year change.

On average being female significantly decreases the probability of diabetes by .051 (p<.001) for white respondents, with a decrease to .015 (p<.001) for nonwhites. The effects of gender differ by .036, which is significant at the .10 level but not the .05 level.

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Comparing DCM_g(x_k) for diabetes

Panel B: DCM for logit model for diabetes (N=16,226).

	White		Nonwhite		Differer	ice
Variable	1: DCM	2: p	3: ADC	4: p	5: ADC	6: p
female	-0.057	<0.001	-0.016	0.431	-0.041	0.070
highschool	-0.038	0.001	-0.029	0.162	-0.008	0.716
married	0.010	0.328	0.013	0.545	-0.003	0.895
ihsincome	-0.025	<0.001	-0.026	<0.001	0.001	0.916
age	0.014	<0.001	0.023	<0.001	-0.009	0.169
active	-0.049	<0.001	-0.083	0.006	0.034	0.319
obese	0.190	<0.001	0.158	<0.001	0.032	0.264

Note: The effect of age is for a five-year change.

1. ADC and DCM do not always lead to the same conclusions as illustrated by the effect of a five-year increase in age.

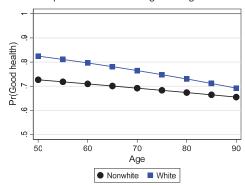
While the ADC of age is significantly larger for nonwhites than whites (p=.002), the effect of age at the mean not differ for whites and nonwhites (p=.169).

2. The different conclusions reflects the different age distributions for whites and nonwhites.

Categorical Data Analysis

Plots: Race, age and good health

1. Do racial disparities in health change with age?



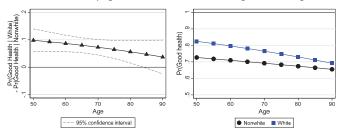
Whites have a higher probability of good health that decreases from .10 at age 50 to less than .04 at 90.

Categorical Data Analysis

Comparing Regressions Across Groups | 32

Are race differences significant?

- 1. We can plot the race difference conditional on age.
 - o When the CI falls below 0, the difference is nonsignificant/
- 2. Racial differences by age show that differences are significant till age 85.



Whites have a higher probability of good health that decreases from .10 at age 50 to less than .04 at 90. Differences are significant at the .05 level until age 85.

Categorical Data Analysis

Comparing Regressions Across Groups | 33

Differences in probabilities and differences in effects

 Since curves are nearly linear, the effects of age can be summarized by changes in the probability of good health as age increase from 50 to 90.

Change over range of age				
1	lincom	pvalue	11	ul
+				
#1 DCage if white	-0.133	0.000	-0.176	-0.089
#2 DCage if nonwhite	-0.072	0.077	-0.151	0.008
#3 DCage race difference	-0.061	0.174	-0.150	0.028

While the effect of age on good health is larger for whites than non-whites, the difference is not significant (p=.17).

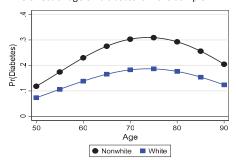
- 2. Levels of health differ significantly, but the effects of age do not.
- 3. We compute these effects by computing differences and second differences in the predicted probabilities.
- 4. The figures for good health show that we do not need the figures!

Categorical Data Analysis

Comparing Regressions Across Groups | 34

Plots: Race, age and diabetes

1. The effect of age on diabetes is more complex.

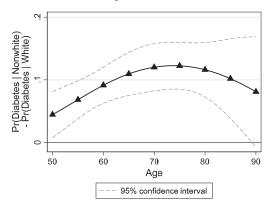


For both groups the probability of diabetes increases from 50 to 75 before declining. While whites have a smaller probability of diabetes at all ages, the difference is smallest at 50 where it is about .04, then increases to a maximum of .12 at 75 before decreasing to .08 at 90.

Categorical Data Analysis

Comparing Regressions Across Groups | 35

2. To determine significance, we plot racial differences with CIs and determine that the differences are significant until about 88.

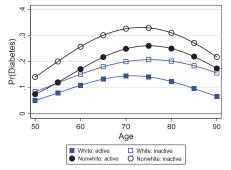


Categorical Data Analysis

Comparing Regressions Across Groups | 36

Plots: Race, age and diabetes by activity

- 1. Are the benefits of activity different for nonwhites and whites?
- 2. Our model includes age and activity in complex ways:
 - c.age c.age#c.age i.active i.active#c.age i.active#c.age#c.ages
- 3. Graphs of probabilities are too complex to understand easily



Categorical Data Analysis

Racial differences with age and activity

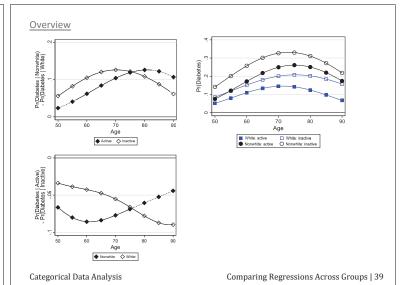
- 1. To simplify, I compute comparisons that emphasize different aspects of our research question.
 - o DCg(race|activity, x)
 - o DC_g(activity|race, x)
- 2. DCg(race|activity, x): racial differences given activity over age
 - o Comparing solid symbols show race differences if active
 - o Comparing hollow symbols show race differences if inactive
- 3. DC_g(activity | race, x): activity differences by race over age
 - o Comparing solid and open squares for activity differences if white
 - o Comparing solid and open squares for activity differences if nonwhite

Avoiding Cls

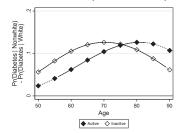
- 4. With multiple lines, CIs can get confusing
- 5. I use a dashed DC line to indicate a difference is NOT significant

Categorical Data Analysis

Comparing Regressions Across Groups | 38



Race differences by level of activity and age

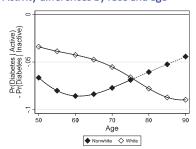


While the benefits of being white occur for those who are active and those who are not, the strength and timing of the benefits differ by level of activity. For those who are not active, the advantages for whites increase from age 50 to 70 before decreasing thereafter. Differences are significant at all ages except 90. For those who are active, the same pattern occurs, but the effects are weaker at younger ages than they are for those who are inactive. The differences increase from age 50 to 80, becoming statistically significant at age 57. At age 80 the differences begin to decrease and are no longer significant.

Categorical Data Analysis

Comparing Regressions Across Groups | 40

Activity differences by race and age



The benefits of activity occur differently for whites and nonwhites. For whites the protective effect of activity is smaller (i.e., less negative) at younger ages and increases in magnitude until age 90. For nonwhites the effect gets stronger from age 50 to 60 before decreasing till age 90; after age 76 the effects are not significant. Tests of racial differences in the effect of activity are significant at the .10 level between ages 55 and 61, reach significance at the .05 level at age 58 where the difference reaches its maximum of .044, and are not significant at other ages.

Categorical Data Analysis

Comparing Regressions Across Groups | 41

Tables: diabetes, gender, and obesity by race

- 1. Do racial differences vary by gender and obesity?
- 2. This is the source data we need to unpack

	W	omen		Men	E	ffect of	obesity	
	1: Obes	e 2: Not	3: Obes	se 4: Not	5: Wome	n 6: Men	7: Diff	
1: White 2: Nonwhite 3: Difference	0.278 0.389 -0.112*	0.107 0.233 -0.126*	0.365 0.408 -0.044	0.152 0.248 -0.096*	0.170* 0.156* -0.014	0.212* 0.161* -0.052†	-0.042* -0.005 -0.038*	

Note: Other variables held at their means.* = p<.01; † = p<.10 for two-tailed test.

3. This complex table is explained on the next page

Unpacking a complicated table

G-gender O-obesit		Girls Women	Boy	s Men	Effect	of obesit	У
R-race	1:Obese	2:Thin	3:Obese	4:Thin	5:Girls	6:Boys	7:Diff
1: Wht 2: Non 3: Dif	π(wgo) π(ngo) Δπ/ΔR go	π(wgt) π(ngt) Δπ/ΔR gt	π(wbo) π(wbo) Δπ/ΔR bo	π(wbt) π(nbt) Δπ/ΔR bo	Δπ/ΔO ng	$\Delta\pi/\Delta0$ nb	Δπ/ΔOG n

Key:

R=race w=white n=nonwhite G=gender b=boy g=girl O=obesity o=obese t=thin $\pi(RGO)$: Prob give R, G and O

 $\Delta\pi/\Delta R$ | GO: Race difference given G and O

 $\Delta\pi/\Delta O \mid RG$: DC(obese) given R and G $\Delta\pi/\Delta OR \mid G$ Race difference in DC(obese) given G

 $\Delta \pi/\Delta OR \mid G$ Race difference in DC(obese) given G $\Delta \pi/\Delta OG \mid R$ Gender difference in DC(obese) given R $\Delta \pi/\Delta OGR$ Race diff in gender diff in obesity difference

4. To simplify $\Delta \pi(female = p, obese = q, \mathbf{x} = \overline{\mathbf{x}})$ is written as $\Delta \pi(female = p, obese = q)$.

Categorical Data Analysis

Comparing Regressions Across Groups | 42

Categorical Data Analysis Comparing Regressions Across Groups | 43

Race differences in diabetes given gender and obesity

1. The last row show estimates of:

$$\frac{\Delta\pi(female = p, obese = q)}{\Delta white}$$

2. We find:

The probabilities of whites being diagnosed with diabetes are smaller than those for nonwhites for all combinations of obesity and gender. The largest racial differences, shown in row 3, is -.126 for women who are not obese and the smallest difference is a nonsignificant -.044 for obese men.

3. To test if racial differences are equal for men and women given obesity, we can compute a second difference (not shown in table):

$$\frac{\Delta\pi(obese=q)}{\Delta female \ \Delta white} = \frac{\Delta\pi(female=1,obese=q)}{\Delta white} - \frac{\Delta\pi(female=0,obese=q)}{\Delta white}$$

The effect of race for obese men and women differ by -.068 = (-.112 - -.044) which is significant at the .02 level. For those who are not obese, the gender difference is smaller and not significant (p=.13).

Categorical Data Analysis

Comparing Regressions Across Groups | 44

Effects of obesity on diabetes

1. To formalize these findings, we estimate DC(obese | gender, race):

$$\frac{\Delta \pi(female = p, white = r)}{\Delta obese}$$

Obesity significantly increases the probability of diabetes by about .16 for all groups except white men where the effect is .21.

2. To test racial differences DC(obese) the last row, columns 5-6:

$$\frac{\Delta\pi(female=p)}{\Delta obese} = \frac{\Delta\pi(female=p, white=1)}{\Delta obese} - \frac{\Delta\pi(female=p, white=0)}{\Delta obese}$$

Racial differences in the effects of obesity are small and not significant for women, but larger and marginally significant for men (p=.09).

3. To gender dofferences DC(obese) using rows 1 and 2 of column 7:

$$\frac{\Delta\pi(\textit{white} = r)}{\Delta\textit{obese}\,\Delta\textit{female}} = \frac{\Delta\pi(\textit{female} = 1, \textit{white} = r)}{\Delta\textit{obese}} - \frac{\Delta\pi(\textit{female} = 0, \textit{white} = r)}{\Delta\textit{obese}}$$

The effect of obesity for whites is .04 larger (p<.001) for men than women, but the gender difference is small and nonsignificant for nonwhite respondents.

Categorical Data Analysis

Comparing Regressions Across Groups | 45

Alternatives when computing effects

- 1. Instead of global means, effects could be computed at local means
- To reflect group differences in the distribution of regressors, compute ADC(obesity) by race and gender.
- 3. The most effective approach for comparing effects depends on the specific questions motivating the research.

Categorical Data Analysis

Comparing Regressions Across Groups | 46

Comparing regression coefficients for diabetes

- 1. Suppose you still want to compare the logit coefficients.
- Consider alternative tests of the hypothesis that the regression coefficients for gender and obesity are equal for whites and nonwhites.
- 3. The of coefficients for diabetes has from standard Wald tests of $H_0:\gamma_k^{\mathrm{W}}=\gamma_k^{\mathrm{N}}$.

If these tests were appropriate, which they are not due to the scalar identification of the coefficients, we would conclude that the protective effects of being female are significantly larger for whites than nonwhites (p<.01) and that the health costs of obesity are significantly greater for whites than nonwhites (p<.01).

4. This contradicts our conclusions using discrete changes.

The ADC for obesity is .022 larger for whites than nonwhites, but the difference is not significant (p=.41); similarly the DCM is .032 larger for whites (p=.26). The ADC and DCM for being female are about .04 less negative for nonwhites than whites, but the differences are not significant (p=.09; p=.07).

Categorical Data Analysis

Comparing Regressions Across Groups | 47

Applying Allison's test

Testing the equality of regression coefficients in models for diabetes

Coefficients constrained to be equal

	Full mc	del	M1: ihs	income	M2: age	, activet	M3: obes	e
Variable	Δβ	p	Δβ	P	Δβ	p	Δβ	p
female obese	-0.321 0.423	0.009	-0.199 0.069	0.164 0.810	-0.363 0.530	0.013 0.064	-0.176 0.000‡	0.120 1.000‡

Note: Results for the full model are from table 3. Tests from models with coefficients constrained to be equal estimated with a location scale model. † All coefficients involving age and/or active are constrained to be equal. † Coefficient for obese are constrained to be equal.

Three equality assumptions we can impose

- o M1: coefficients for ihsincome are constrained to be equal;
- o M2: coefficients that include age or active are constrained
- o M3: coefficients for obese are constrained.
- o Models with other constrains did not converge.

Racial differences in regression coefficients for *female*

o M1: p=.164

o M2: p=.013

o M3: p=.120

Racial differences in regression coefficients for obese

o M1: p=.810

o M2: p=.064

The models are empirically indistinguishable

- o The predictions from M1 and M3 are identical
- \circ The predictions for M3 have correlations of about .999

Categorical Data Analysis

Comparing Regressions Across Groups | 48

Categorical Data Analysis

Code for comparing groups

Joint fitting models using factor syntax

logit goodhlth ibn.white ///

ibn.white#(i.female ... i.obese), nocon

- o **ibn** means indicator variable where you want dummies for both values
- o ibn.white: estimates intercepts for both groups
- o ibn.white#(i.female ... i.obese): intercations with regressors
- o nocon : do not include intercept

Example of output:

```
goodhlth
                   Coef.
      white |
  Nonwhite
               -1.541056 : Nonwhite intercept
               -.4880763 : White intercept
     White
white#female
   Nonwhite#
    Female |
               -.1183793 : Nonwhite \beta for female
```

Categorical Data Analysis

Comparing Regressions Across Groups | 50

White#Female | .1437669 : White β for female

- o white is the variable with values Nonwhite and White
- o white#female is the interaction of white with female
- o Nonwhite#Female interacts female with being nonwhite and is 0 for those who are white
- o White#Female interacts female with being white and is 0 for those who are nonwhites

Categorical Data Analysis

Comparing Regressions Across Groups | 51

Computing marginal effects

Comparing ADC for indicator variables

- 1. over(white) averages over the groups defined by white
- . est restore fullmodel
- . mtable, dydx(female) over(white) post brief dec(4)

Expression: Pr(diabetes), predict()

	d Pr(y)
Nonwhite	
White	-0.0506

- 2.mlincom creates a table with 1st and 2nd differences
- . qui mlincom (2), rowname(ADC female: White) add clear
- qui mlincom (1), rowname(ADC female: Nonwhite) add . mlincom (2-1), rowname(ADC female: Difference) twidth(25) add

	!	lincom	pvalue	11	ul
ADC female	i				
	White	-0.051	0.000	-0.066	-0.036
	Nonwhite	-0.015	0.431	-0.053	0.023
	Difference	-0.036	0.089	-0.077	0.006

Categorical Data Analysis

Comparing Regressions Across Groups | 52

Comparing ADC from continuous variables

- 1.at(age=gen(age)) computes predictions at observed age
- 2.at(age=gen(age+5)) computes predications at 5 plus observed age
- . est restore fullmodel
- . mtable, at(age=gen(age)) at(age=gen(age+5)) over(white) post

	PI(Y)
0.white#c.1	0.2811
1.white#c.1	0.1615
0.white#c.2	0.3080
1.white#c.2	0.1729

- 3. Compute the effects
- . qui mlincom (4-2), rowname(ADC age+5: White) clear
- . qui mlincom (3-1), rowname(ADC age+5: Nonwhite) add . mlincom (4-2) (3-1), ///
- rowname(ADC age+5: Difference) twidth(25) add

	lincom	pvalue	11	ul
ADC age+5	i			
White	0.011	0.000	0.008	0.015
Nonwhite	0.027	0.000	0.018	0.036
Difference	-0.016	0.002	-0.025	-0.006

Categorical Data Analysis

Comparing Regressions Across Groups | 53

Compare DCM for female

- . est restore fullmodel
- mtable, dydx(female) post at((omeans) _all white=(0 1))

Expression: Pr(diabetes), predict()

!	white	d Pr(y)
1	0	-0.0160
2	1	-0.0573

Specified values of covariates

	1.	1.	1.			1.
	female	highsc~l	married	ihsinc~e	age	active
Current	.5392	.805	.6667	4.405	66.11	.29
::						

- . qui mlincom (2), rowname(DCM female: White)
 . qui mlincom (1), rowname(DCM female: Nonwhite)
 . mlincom (2-1), rowname(DCM female: Difference) add add clear

Compare DCM for age

- 1. Get start and end values
- . svy: mean age // compute start and end for age

							nterval]
age	66.	11455	.1723	443	65.7	693	66.4598

- . global ageST = _b[age] // mean
 . global ageEN = _b[age] + 5 // mean + 5
- 2. Predictions where (omeans) _all is the overall means . mtable, at((omeans) _all age=(\$ageST \$ageEN) white=(0 1)) post dec(4)

Expression: Pr(diabetes), predict()

 	white	age	Pr(y)	
1	0	66.11	0.2832	
2	0	71.11	0.3063	
3	1	66.11	0.1706	
Δĺ	1	71 11	0 1849	

Specified values of covariates

Categorical Data Analysis

Comparing Regressions Across Groups | 55

Categorical Data Analysis

```
3. First and second differences:
```

```
rowname(DCM age+5: White)
rowname(DCM age+5: Nonwhite)
 qui mlincom (4-3),
. mlincom (4-3) - (2-1), rowname(DCM age+5: Difference) add
```

	lincom	pvalue	11	ul
DCM age+5	i			
White	0.014	0.000	0.009	0.019
Nonwhite	0.023	0.000	0.011	0.035
Difference	-0.009	0.169	-0.021	0.004

Categorical Data Analysis

Comparing Regressions Across Groups | 56

Plots

```
Plotting predictions
```

```
mgen, at(white=1 age=(50(5)90)) atmeans stub(AprW) ///
    predlabel(White) replace // probabilities for whites
mgen, at(white=0 age=(50(5)90)) atmeans stub(AprN) ///
     predlabel(Nonwhite) replace // probabilities for nonwhites
// plot probabilities
twoway ///
     (connected AprWprl AprWage, $LINwht) ///
      (connected AprNpr1 AprWage, $LINnon) ///
      (scatter
                     AprWprl AprWage, $LINwht) ///
AprNprl AprWage, $LINnon), ///
     (scatter
     ytitle(Pr(Good health)) xtitle(Age) ///
xlab(50(10)90) ylab(.5(.1)1, gmin gmax grid) ///
yline(1, lcol(black) lwid(*.6)) legend(rows(1) order(4 3)) ///
     scale(1.2)
```

Categorical Data Analysis

Comparing Regressions Across Groups | 57

```
Plot group differences
```

```
mgen, dydx(white) at(age=(50(5)90)) atmeans stub(Adc) ///
predlabel(DC) replace // DCrace
label var Adcull "95% confidence interval"
label var Adcull "95% confidence interval"
   to reverse directory of DC
gen RAdcd_prl = -1 * Adcd_prl
gen RAdcll1 = -1 * Adcll1
gen RAdcul1 = -1 * Adcul1
label var Adcll1 "95% confidence interval"
twoway ///
                                                            Adcage, $LINdc) /// line
        (connected Adcd_pr1
       (connected Adc1l1 Adcul1 Adcage, $LINci) /// ci
(scatter Adcd_prl Adcage, $LINdc), /// line
ytitle("Pr(Good Health | White)" "- Pr(Good Health | Nonwhite)") ///
               title(*P(GOOD health | White) = F(GOOD health | No.
xtitle(Age) xlab(50(10)90) ylab(-1(.1).2, grid) ///
yline(-.1 .2, lcol(black*.2) lwid(*.7)) ///
                legend(pos(6) ring(1) cols(1) order(3) symxsize(7)) ///
scale(1.2) ///
                yline(0, lcol(black) lwid(*.6))
```

Categorical Data Analysis

Comparing Regressions Across Groups | 58

Computing change over range of age

. mtable, at(age=(50 90) white=(0 1)) atmeans post

Expression: Pr(goodhlth), predict()

	white	age	Pr(y)
1	0	50	0.727
2	0	90	0.655
3	1	50	0.825
4	1	90	0.692

. qui mlincom (4-3), rowname(#1 DCage if white) clear . qui mlincom (2-1), rowname(#2 DCage if nonwhite) add . mlincom (4-3)-(2-1), rowname(#3 DCage race difference) add

Categorical Data Analysis

Comparing Regressions Across Groups | 59

Tables

1. To examine if racial differences vary by gender and obesity:

V	Women		Men E		ffect of obesity	
1: Obes	e 2: Not	3: Obes	e 4: Not	5: Wome	 n 6: Men	7: Diff
1: White 0.278	0.107	0.365	0.152	0.170*	0.212*	-0.042*
2: Nonwhite 0.389	0.233	0.408	0.248	0.156*	0.161*	-0.005
3: Difference -0.112*	-0.126*	-0.044	-0.096*	-0.014	-0.052†	-0.038*
Note: Other variables held at their means *-nc 01: t-nc 10 for two-tailed test						

- o Probabilities are in rows 1-2, columns 1-4
- o Row 3 is racial differences in probabilities given obesity and gender
- o Columns 5-6 are DCs of obesity given gender
- o Column 7 compare DCs of obesity for men and women
- 2. To simplify $\Delta\pi(female = p, obese = q, \mathbf{x} = \overline{\mathbf{x}})$ is written as $\Delta\pi(female = p, obese = q)$.

Categorical Data Analysis

Comparing Regressions Across Groups | 60

```
Code: Pr(diabetes | female, obese, race)
```

```
. // #3.1 Pr(diabetes | female, obese, race)
```

- . // Table 4 rows 1-2, columns 1-4
- . qui est restore fullmodel
- . // Pr(diabetes | female, obese, race)
- . mtable, at(white=(0 1) female=(0 1) obese=(0 1)) atmeans stats(est

Expression: Pr(diabetes), predict()

	. !	white		obese		p
		0				0.000
::			_		0.000	

Specified values of covariates

1	1.	1.			1.
į	highsc~l	married	ihsinc~e	age	active
Current	.805	. 667	4.41	66.1	. 29

Categorical Data Analysis

```
Code: DC(race | female, obese)
```

```
. // #3.2 Race dif by gender and obesity: DC(race | female, obese)
. // Table 4 row 3, columns 1-4
```

. mtable, dvdx(white) at(female=(0 1) obese=(0 1)) /// atmeans stats(est pvalue) post

Expression: Pr(diabetes), predict()

		female	obese	d Pr(y)	P
	1	0	0	-0.096	0.000
::	4	1	1	-0.112	0.000

Specified values of covariates

Categorical Data Analysis

Comparing Regressions Across Groups | 62

Code: DC(race | female, obese) by gender or obesity

```
#3.2a Compare DC(race | female, obese) across gender and obesity Table 4 row 3, columns 5-6 are from rows 3 and 4 below
```

men - obese . qui mlincom 4-2, rowname(obese women) . qui mlincom 3-1, rowname(nonobese men - nonobese women) add

qui mlincom 4-3, rowname(women obese - women nonobese) add qui mlincom 2-1, rowname(men obese - men nonobese) add

mlincom, twidth(32) title(Second differences in DCobese and DCfemale)

Second differences in DCobese and DCfemale

	lincom	pvalue	11	ul
obese men - obese women nonobese men - nonobese women women obese - women nonobese	-0.068 -0.030 0.014	0.019 0.126 0.603	-0.124 -0.070 -0.041	-0.012 0.009 0.069
men obese - men nonobese	0.052	0.086	-0.008	0.111

Categorical Data Analysis

Comparing Regressions Across Groups | 63

Code: DC(obese | female, race) by gender or race

```
. // #3.3 DC(obesity | race gender)
. // Table 4 rows 1-2, columns 5-6
```

. qui est restore fullmodel
. mtable, dydx(obese) at(white=(0 1) female=(0 1)) /// atmeans stats(est pvalue) post

Expression: Pr(diabetes), predict()

	white	female	d Pr(y)	p
1	0	0	0.161	0.000
2	j 0	1	0.156	0.000
3	1	0	0.212	0.000
4	i 1	1	0 170	0 000

Specified values of covariates

Categorical Data Analysis

Comparing Regressions Across Groups | 64

```
. // 3.3a Additional tests: requires Stata 14.2+ due to bug in 14.1
. // DC of obesity are equal across race and gender . test [1.obese]1bn._at = [1.obese]2._at = [1.obese]3._at = [1.obese]4._at
```

(1) [1.obese]lbn._at - [1.obese]2._at = 0 (2) [1.obese]lbn._at - [1.obese]3._at = 0 (3) [1.obese]lbn._at - [1.obese]4._at = 0

3, 54) = 12.42 Prob > F = 0.0000

. // Compare DC of obesity for nonwhite men and white women

. test [1.obese]1bn._at = [1.obese]4._at, accum

Adjusted Wald test

Adjusted Wald test

(1) [1.obese]1bn._at - [1.obese]2._at = 0

(2) [1.obese]lbn._at - [1.obese]3._at = 0
(3) [1.obese]lbn._at - [1.obese]4._at = 0
(4) [1.obese]lbn._at - [1.obese]4._at = 0
Constraint 4 dropped

F(3, 3, 54) = 12.42 Prob > F = 0.0000

Categorical Data Analysis

Comparing Regressions Across Groups | 65

```
#3.4 Second and third differences to compare effects
```

. // Table 4 rows 1-3, column 7

qui mlincom 2-4, rowname(D2race|fem) clear

qui mlincom 1-3, rowname(D2race mal) add qui mlincom 4-3, rowname(D2gndr|wht) add

qui mlincom 2-1, rowname(D2gndr|non) add mlincom (4-3)-(2-1), rowname(D3gndrXrace) add

I	lincom	pvalue	11	ul
D2race fem D2race mal D2gndr wht D2gndr non D3gndrXrace	-0.014 -0.052 -0.042 -0.005 -0.038	0.603 0.086 0.000 0.428 0.000	-0.069 -0.111 -0.056 -0.016 -0.057	0.041 0.008 -0.028 0.007 -0.019

Conclusions

- 1. I recommend comparing groups using predictions and marginal effect on predictions in of outcomes measured in a natural metric.
- 2. This approach
 - o Identification is not a concern
 - $\circ\,$ The method can be applied to any regression model that makes predictions : it is useful in any nonlinear model including LRM
 - o Any number of groups can be included
- 3. Deciding how to make comparisons requires careful consideration based on a substantive understanding of the process being modeled and the questions being asked.

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Categorical Data Analysis

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Chow, G.C. 1960. Tests of equality between sets of coefficients in two linear

Categorical Data Analysis

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Long, J.S. 2009 (2005). Comparing groups using predicted outcomes. (www.indiana.edu/~jslsoc/research_groupdif.htm)

Long and Mustillo. 2018. Using predictions to compare groups in regression models for binary outcomes

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Comparing Regressions Across Groups | 68

TODO Oaxaca Decomposition

- 1. See in Resources the rough draft
- 2. Search Groups for computer code and didactic figures
- 3. Citation to Jann article

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Comparing Regressions Across Groups | 69

Example: productivity, position, and tenure

Variable	Mean	StdDev	Minimum	Maximum	Label
tenure	0.12	0.33	0.00	1.00	Is tenured?
female	0.38	0.48	0.00	1.00	Scientist is female?
year	3.86	2.30	1.00	10.00	Years in rank.
yearsq	20.17	22.15	1.00	100.00	Years in rank squared.
select	5.00	1.41	1.00	7.00	Selectivity of bachelor's
articles	7.05	6.58	0.00	73.00	Total number of articles.
prestige	2.65	0.78	0.65	4.80	Prestige of department.
presthi	0.05	0.21	0.00	1.00	Prestige is 4 or higher?

N = 2797 (person-years)

Categorical Data Analysis

Comparing Regressions Across Groups | 70

Model for women

logit (N= 2797): Factor Change in Odds

WOMEN	b	z	P> z	e^b	e^bStdX
constant	-5.84198	-6.747	0.000	0.0029	0.0589
year	1.40777	5.472	0.000	4.0868	30.1273
yearsq	-0.09559	-4.364	0.000	0.9088	0.1857
select	0.05513	0.769	0.442	1.0567	1.1534
articles	0.03395	2.693	0.007	1.0345	1.2181
prestige	-0.37079	-2.376	0.017	0.6902	0.6013
MEN	b	z	P> z	e^b	e^bStdX
	7 69016	11 071	0 000	0 0005	0 0241

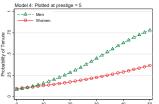
MEN	b	z	P> z	e^b	e^bStdX	
constant	-7.68016	-11.271	0.000	0.0005	0.0241	
year	1.90885	8.915	0.000	6.7454	130.9789	
yearsq	-0.14322	-7.699	0.000	0.8666	0.0622	
select	0.21577	3.513	0.000	1.2408	1.7711	
articles	0.07369	6.367	0.000	1.0765	1.5299	
prestige	-0.43119	-3.963	0.000	0.6497	0.5418	

Categorical Data Analysis

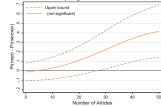
Comparing Regressions Across Groups | 71

Articles with prestige = 5 (elite) other variables at means

A. Probabilities by gender



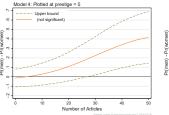
B. Group differences with CI



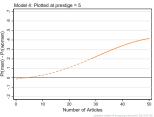
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Converting CI to a broken line

B. Group difference with CI



C. Group difference with broken line

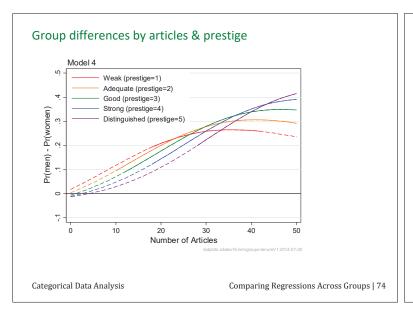


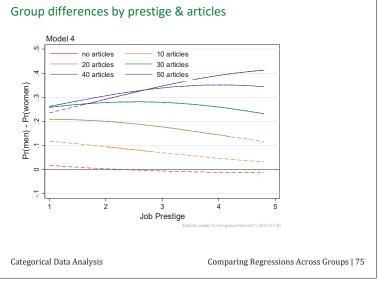
- o Do this for each level of prestige
- o Then combine the group differences in a single graph

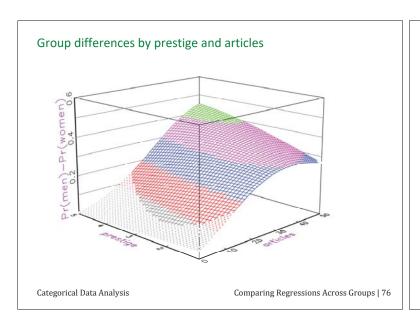
Categorical Data Analysis

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Categorical Data Analysis







β1a Comparing Effects Across Equations

Readings and examples

Trent Mize, Long Doan, and Scott Long. 2018. A General Framework for Comparing Marginal Effects Across Models. Working paper.

See references in Mize et al.

mdo18-cme-*.do: do-files take several minutes to complete.

Categorical Data Analysis

Comparing Effects Across Equations | 1

Overview: comparing effects across models

- 1. Statistical issues
 - o Jointly fit multiple models
 - o Jointly estimate effects with standard errors and covariances
 - o Test equality of effects across models
- 2. Practically issues
 - o Software must be able to jointly fit models and estimate effects

Examples

- 1. Can the relationship between two variables be explained by adding controls?
- 2. Does a different operationalization change the effect of interest?
- 3. Is a treatment more effective helpling for depression or impulse control?
- 4. Do conclusion from a Pew survey match those from the GSS?
- 5. Does the effect of age depend on whether the model is ordinal or nominal?
- 6. Are effects of age greater in cubic model than quadratic model?

Categorical Data Analysis

Comparing Effects Across Equations | 2

Review of Marginal Effects

- 1. Consider any regression model
 - $\eta(\mathbf{x}) = G(\mathbf{x}\boldsymbol{\beta})$
- 2. Examples include:
- o For BLM, $Pr(\mathbf{x}) = \Lambda(\mathbf{x}\boldsymbol{\beta})$
- o For LRM, $y = x\beta + \varepsilon$
- o MNLM, OLM, NBRM, or nearly any other model
- 3. The marginal effect is the change in η for a change in x_k holding other variables at specific values.

Categorical Data Analysis

Discrete change at representative values (DCR)

1. Change in η as x_k changes from *start* to *end* holding other variables at x^* :

$$\frac{\Delta \eta(\mathbf{x} = \mathbf{x}^*)}{\Delta x_k(start \rightarrow end)} = \eta(x_k = end, \mathbf{x} = \mathbf{x}^*) - \eta(x_k = start, \mathbf{x} = \mathbf{x}^*)$$

$$\frac{\Delta \eta(\mathbf{x} = \overline{\mathbf{x}}^*)}{\Delta x_k(\overline{x}_k \to \overline{x}_k + s_k)} = \eta(x_k = \overline{x}_k + s_k, \mathbf{x} = \overline{\mathbf{x}}^*) - \eta(x_k = \overline{x}_k, \mathbf{x} = \overline{\mathbf{x}}^*)$$

$$\frac{\Delta \eta(\mathbf{x} = \mathbf{x}^*)}{\Delta x_{k}(0 \to 1)} = \eta(x_{k} = 1, \mathbf{x} = \mathbf{x}^*) - \eta(x_{k} = 0, \mathbf{x} = \mathbf{x}^*)$$

Categorical Data Analysis

Comparing Effects Across Equations | 4

Average discrete change (ADC)

1. DC_i(x_k) for each observation i:

$$\frac{\Delta \eta(\mathbf{x} = \mathbf{x}_i)}{\Delta x_k(start_i \rightarrow end_i)} = \eta(x_k = end_i, \mathbf{x} = \mathbf{x}_i) - \eta(x_k = start_i, \mathbf{x} = \mathbf{x}_i)$$

$$\frac{\Delta \eta(\mathbf{x} = \mathbf{x}_i)}{\Delta x_k(x_{ik} \to x_{ik} + \delta)} = \eta(x_k = x_{ik} + \delta, \mathbf{x} = \mathbf{x}_i) - \eta(x_k = x_{ik}, \mathbf{x} = \mathbf{x}_i)$$

$$\frac{\Delta \eta(\mathbf{x} = \mathbf{x}_i)}{\Delta x_k(start \rightarrow end)} = \eta(x_k = end, \mathbf{x} = \mathbf{x}_i) - \eta(x_k = start, \mathbf{x} = \mathbf{x}_i)$$

2. $ADC(x_k)$ is the average discrete change

$$ADC_{x_k} = \frac{1}{N} \sum_{i} \frac{\Delta \eta(\mathbf{x} = \mathbf{x}_i)}{\Delta x_k(start_i \rightarrow end_i)})$$

- 3. Average can over:
 - o entire sample
 - o subsamples (e.g, men and women)

Categorical Data Analysis

Comparing Effects Across Equations | 5

Testing the equality of effects

- 1. Models:
 - o M1: logit of satisfaction on education plus controls
 - o M2: logit of satisfaction on income plus controls
- 2. Jointly fit M1 and M2 and estimate effects (ADC, DCR, RRR,...)
 - $\circ \Delta_1 = ADC(education)$ from M1
 - \circ Δ_2 = ADC(income) from M2
- 3. Wald test statistic for Ho: $\Delta_1 = \Delta_2$

$$z = \frac{\hat{\Delta}_1 - \hat{\Delta}_2}{\sqrt{\hat{\sigma}_1^2 + \hat{\sigma}_2^2 - 2\hat{\sigma}_{1,2}}}$$

- 4. $\hat{\sigma}_{\scriptscriptstyle 1,2}$ usually requires joint fitting of models and estimation of effects
- 5. Standard error computed with delta method, bootstrapping, or simulation.
- 6. Joint estimation is completed using SUEST

Categorical Data Analysis

Comparing Effects Across Equations $\mid 6$

Joint fitting with seemingly unrelated estimation (SUEST)

Adapted from Wessie (1999)

Unstacked data of N observations

- 1. Fit two models
 - o Model 1: regress depress roles
 - o Model 2: regress sick roles
- 2. We can estimate and test individual effects but not compare them.

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Comparing Effects Across Equations | 7

Stacked data of 2N observations

(y	rolesm1	rolesm2	is model 1	id \
depress = 0	5	0	1	1
depress = 1	1	0	1	2
:	:	:	:	
depress = 1	8	0	1	N
sick = 0	0	5	0	1
sick = 1	0	1	0	2
:	:	:	:	
sick = 1	0	8	0	N

y First N rows are depress from unstacked data; last N rows are sick rolesm1 First N rows are roles from unstacked dataset; last N fixed to 0. rolesm2 First N rows are 0; last N contain roles from unstacked dataset

1 if observation for Model 1; 2 if observation for Model 2

Fitting models with stacked data

1. Fit models separately

logit y rolesm1 if ismodel1==1
logit y rolesm2 if ismodel1==2

2. To fit model jointly

logit y ismodel2 rolesm1 rolesm2, vce(cluster id)

- o ismodel1 is 1 if the observation is needed to fit model 1 and 0 if the observation is used to fit model 2.
- id is used to adjust for clustering caused by having two observations for each participant.
- o vce(cluster id)adjust for the clustered data
- 3. Example of results of using stacked data follows...

Categorical Data Analysis

ismodel1

Comparing Effects Across Equations | 8

Categorical Data Analysis

Estimates fi	Estimates from Models 1 and 2 fit separately and jointly						
Outcome:	Model 1 depress	Model 2 sick	Model 3 Both				
roles	-0.2006 (0.0252)	-0.2608 (0.0365)					
rolesm1			-0.2006 (0.0257)				
rolesm2			-0.2608 (0.0371)				
ismodel1			-0.8115 (0.2311)				
Constant	-0.0401 (0.1478)	-0.8516 (0.2065)	-0.0401 (0.1503)				
N	4,307	4,307	8,614				

Categorical Data Analysis

Comparing Effects Across Equations | 10

SUEST and generalized SEM

- 1. Stacking data only works if models are the same type (e.g., two logits)
- 2. SUEST is a statistical method that is a more general way to "stack" results to combines estimates across models to obtain correct SE's
- 3. After joint estimation, marginal effects can be jointly estimated across models
- 4. SEM programs, like gsem, can also be used to jointly fit models
 - o suest is faster and more general, but postestimation is messy
 - \circ gsem is much slower but eaiser to use for postestimation

Categorical Data Analysis

Comparing Effects Across Equations | 11

Examples and Applications

- 1. Compare effects across nested models
- \circ Does the effect of a x_k changes as controls are added to the model?
- 2. Compare effects of different operationalizations of a variable.
- o Does the way sexual orientation is measured change its effects?
- 3. Compares effects of the same predictor on different outcomes.
 - o Does gender have the effect on diabetes as arthritis?
- 4. Group comparisons is a special case of this method.
- 5. Compare effects of x_k in OLM to the effect of x_k in MNLM
- 6. Does the effect of age in a model with age-squared differ from the effect in a model that adds age-cubed?

Categorical Data Analysis

Comparing Effects Across Equations | 12

Mediation of effects using nested logit models

- 1. People with college degrees tend to be happier than those without.
- 2. Does the effect of a college degree change after accounting for earnings, occupational prestige, and other variables?

Data and variables from GSS 2000-2016

Variable	Unique	Mean	Min	Max	Label
vhappy	2	.3087023	0	1	Very Happy with Life
college	2	.3390842	0	1	R Has College Degree
wages	2936	17.4244	.111	5278	70 Wages
occprest	62	45.31217		16	86 Occupational Prestige Score
married	2	.4950087	0		1 Currently Married
parent	2	.6885851	0		1 Parent
woman	2	.4930556	0		1 Woman R
conserv	2	.335612	0		1 Conservative R
reltrad	7	3.650282	1		7 Religous Tradition
year	9	2008.175	2000	201	6 gss year for this respondent
age	71	42.94477	18	8	8 age of respondent

Categorical Data Analysis

Comparing Effects Across Equations | 13

Models

M1: vhappy on college

M2: vhappy on college + controls

M3: vhappy on college + controls + wages

M4: vhappy on college + controls + wages + occprest

Results: ADC(college) on happiness

Panel	A:	ADC(college)

	Model 1:	Model 2:	Model 3:	Model 4:
	College	+ Controls	+ Wages	+ Prestige
ADC(college)	0.072***	0.060***	0.036***	0.019 (0.012)

Panel B: Cross Model Differences

	Model 1:	Model 2:	Model 3:	Model 4:
Model 1		0.012** (0.004)	0.036*** (0.006)	0.053*** (0.007)
Model 2	0.012** (0.004)		0.024*** (0.004)	0.041*** (0.006)
Model 3	0.036*** (0.006)	0.024*** (0.004)		0.017*** (0.004)
Model 4	0.053*** (0.007)	0.041*** (0.006)	0.017*** (0.004)	

Notes:Standard errors in parentheses. *=p≤.05, **=p≤.01, ***=p≤.001 for a two-tailed test.

Categorical Data Analysis

Model 1 with only college as predictors

On average the probability of being happy is .072 (p<.001) higher for those with a college degree.

Model 2 adds control variables

Adding the controls decreases the effect of college by .012 (p<.001).

Model 3 examines if effect of college is mediated by hourly wages.

After controlling for wages, the effect of college continues to be significant (Δ =.036, p<.001), but is reduced by .024.

Model 4 adds wages as a mediator.

On average going to college increase the probability of a respondent reporting being very happy by .019 which is no long34 significant.

Overall, we can conclude

The relationship between a college degree and happiness is totally moderated by wages and prestige.

Categorical Data Analysis

Comparing Effects Across Equations | 16

Fit models separately and estimates effects of college

```
local controls ///
    i.married i.parent i.woman i.conserv i.reltrad i.year c.age##c.age
logit vhappy i.college // M1
mchange college, stat(est se p) dec(7)
logit vhappy i.college `controls' // M2 + controls
mchange college, stat(est se p)
logit vhappy i.college c.wages `controls' // M3 + wages
mchange college wages , amount(sd) stat(est se p)
logit vhappy i.college c.wages c.occprest `controls' // M4 + occprest
mchange college wages occprest, amount(sd) stat(est se p)
```

Categorical Data Analysis

Comparing Effects Across Equations | 17

Joint fitting of models

Clones to trick gsem into using the same DV in all models

```
clonevar vhappyM1 = vhappy
lab var vhappyM1 "M1 vhapppy college only"
vhappyM2 = vhappy
lab var vhappyM3 = vhappy
vhappyM3 = vhappy
lab var vhappyM3 "M2 vhapppy college + controls"
clonevar vhappyM3 "M3 vhapppy college + controls + wages"
clonevar vhappyM4 = vhappy
lab var vhappyM4 "M4 vhapppy college + controls + wages + occprest"
// NOTE: vce(robust) needed for correct covariances across models

Simultaneously fit models with gsem

gsem (vhappyM1 <- i.college, logit) ///
    (vhappyM3 <- i.college controls', logit) ///
    (vhappyM3 <- i.college c.wages `controls', logit) ///
    (vhappyM4 <- i.college c.wages c.occprest `controls', logit) ///
    , vce(robust)

est store gsemmodel
```

Categorical Data Analysis

Comparing Effects Across Equations | 18

Jointly estimate ADC(college) and post results

. margins, dydx(college) post

```
Average marginal effects Number of obs = 9,216

dy/dx w.r.t. : 1.college
1._predict : Predicted mean (M1 vhapppy college only), predict(mu
outcome(vhappyM1))

2._predict : Predicted mean (M2 vhapppy college + controls), predict(mu
```

2._predict : Predicted mean (M2 vhapppy college + controls), predict(routcome(vhappyM2))
 3._predict : Predicted mean (M3 vhapppy college + controls + wages), predict(mu outcome(vhappyM3))

predict(mu outcome(vhappyM3))
4._predict : Predicted mean (M4 vhappy college + controls + wages +
occprest), predict(mu outcome(vhappyM4))

	dy/dx	Delta-method Std. Err.	z	P> z	[95% Conf.	Interval]
0.college	(base outco	ome)				
1.college _predict	 					
1	.071806	.0103344	6.95	0.000	.0515509	.0920611
2	.0599197	.0105299	5.69	0.000	.0392813	.080558
3	.0359563	.0111027	3.24	0.001	.0141954	.0577172
4	.0191807	.0117766	1.63	0.103	003901	.0422625

Note: dy/dx for factor levels is the discrete change from the base level.

Categorical Data Analysis

est restore gsemmodel

Comparing Effects Across Equations | 19

Compute ADC(college) and second differences across models

```
qui mlincom 1, rowname(ADCcollege: M1)
                                                             stat(est se p) clear
                      rowname(ADCcollege: M2)
                                                             stat(est se p) add
qui mlincom 1-2, rowname(ADCcollege: M1 - M2) stat(est se p) add
qui mlincom 1, rowname(ADCcollege: M1) stat(est se p) add qui mlincom 3, rowname(ADCcollege: M3) stat(est se p) add
qui mlincom 1-3, rowname(ADCcollege: M1 - M3) stat(est se p) add
qui mlincom 1, rowname(ADCcollege: M1)
qui mlincom 4, rowname(ADCcollege: M4)
                                                            stat(est se p) add
                                                            stat(est se p) add
qui mlincom 1-4, rowname(ADCcollege: M1 - M4) stat(est se p) add
qui mlincom 2, rowname(ADCcollege: M2)
qui mlincom 3, rowname(ADCcollege: M3)
                                                            stat(est se p) add
                                                             stat(est se p) add
qui mlincom 2-3, rowname(ADCcollege: M2 - M3) stat(est se p) add
qui mlincom 2, rowname(ADCcollege: M2)
qui mlincom 4, rowname(ADCcollege: M4)
                                                            stat(est se p) add
                                                             stat(est se p) add
qui mlincom 2-4, rowname(ADCcollege: M2 - M4) stat(est se p) add
qui mlincom 3, rowname(ADCcollege: M3) stat(est se p) add qui mlincom 4, rowname(ADCcollege: M4) stat(est se p) add mlincom 3-4, rowname(ADCcollege: M3 - M4) stat(est se p) add twidth(15)
```

Categorical Data Analysis

ADC(wages+SD) for models 3 and 4

Categorical Data Analysis Comparing Effects Across Equations | 21

Effects of alternative regressors

- 1. Sexual orientation can be measured in different ways.
 - How someone identifies with an orientation
 - o How someone behaves
- 2. Does classifying sexual orientation based on their *identity* leads to different conclusions than classifying based on *behavior*?

Data and variables: GSS data from 2008 - 2016

- Outcome is whether a person views same-sex relationships as wrong (=1) or not wrong (=0).
- 2. Sexual orientation *identity* and sexual orientation *behavior* have three categories
 - o heterosexual
 - o bisexual
 - o gay/lesbian.

Categorical Data Analysis

Comparing Effects Across Equations | 22

Logit model of same-sex is wrong on orientation + controls

M1: sexual identity

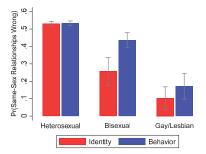
iswrong <- sexident woman college age race year M2: sexual behavior

iswrong <- sexbehav woman college age race year

Categorical Data Analysis

Comparing Effects Across Equations | 23

Pr(iswrong) by sexual orientation measured two ways



Views of same-sex relationships are nearly identical across models for those who identify as heterosexual, fairly close for those who identify as gay or lesbian, but the probability of viewing same-sex relationships as wrong is substantially lower for those who are classified as bisexual based their sexual identity compared to past sexual behavior.

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Comparing Effects Across Equations | 24

Pr(iswrong) by sexual orientation measured two ways

Here are the numbers behind the prior graph

Orientation	Model 1: Sexual Identity	Model 2: Sexual Behavior	Cross Mode Difference
Heterosexual	0.531	0.533	0.002 (0.002)
Bisexual	0.257	0.436	0.179*** (0.041)
Gay/Lesbian	0.104	0.171	0.067 (0.040)

The probability of bisexuals saying same-sex relationships are wrong are significantly larger when orientation is measured by behavior than by identity (p<.001). The probabilities for heterosexuals and gay/lesbians do not differ significantly.

Categorical Data Analysis

Comparing Effects Across Equations | 25

ADC(sexual orientation) comparing two orientations

	Model 1: Sexual Identity	Model 2: Sexual Behavior	Cross Model Difference
Heterosexual vs Bisexual	-0.274***	-0.097***	0.177***
	(0.041)	(0.023)	(0.043)
Heterosexual vs Gay/Lesbian	-0.428***	-0.362***	0.066
	(0.034)	(0.038)	(0.041)
Bisexual vs Gay/Lesbian	-0.265**	-0.153*	-0.111
	(0.044)	(0.052)	(0.059)

*=p=.05, **=p=.01, ***=p=.001 for a two-tailed test

The contrast between heterosexual and gay/lesbian and between bisexual and gay/lesbian do not differ significantly across the two models. However, there is a significantly larger difference between heterosexual and bisexual individuals when using the sexual identity measure compared to , compared sexual behavior measure. That is, for this contrast the different ways of measuring sexual orientation change the effect.

Is this clear?

Categorical Data Analysis

Comparing Effects Across Equations | 26

Version 1 confuses me!

The contrast between heterosexual and gay/lesbian and between bisexual and gay/lesbian do not differ significantly across the two models. However, there is a significantly larger difference between heterosexual and bisexual individuals when using the sexual identity measure compared to , compared sexual behavior measure. That is, for this contrast the different ways of measuring sexual orientation change the effect.

Version 2: is this better?

The effect of being heterosexual compared to being gay or lesbian does not differ when sexual orientation is measured by behavor or identity. However, the effect of being heterosexual compared to bisexual is significantly larger (p<.001) when orientation is measured by sexual identity.

Categorical Data Analysis

Code for example

Jointly fit models

Categorical Data Analysis

Comparing Effects Across Equations | 28

Estimate and plot probabilities by orientation

```
// model using behavior
est restore gsemmodel
margins, predict(outcome(samesexBEHAV)) at(sexbehav=(1 2 3)) post
est store probbehav
// model using identity
est restore gsemmodel
margins, predict(outcome(samesexIDENT)) at(sexident=(1 2 3)) post
est store probident

local labopt "labsize(*1.1) glwidth(*1.4) glcol(black*.7)"

coefplot (probident, color(red*.8)) (probbehav, color(black)), ///
    vertical recast(bar) barw(0.3) ///
    ciopts(recast(rcap) color(gs8)) citop ///
    legend(order(1 "Identity" 3 "Behavior")) ///
    xlab(1 "Heterosexual" 2 "Bisexual" 3 "Gay/Lesbian", noticks) ///
    ytitle("Pr(Same-Sex Relationships Wrong)",size(*.85)) ///
    ylab(0(0.1).6, "labopt') ///
    scale(1.3) /// larger text
    xscale(noline) plotregion(style(none)) // turn off x axis line
```

Categorical Data Analysis

Comparing Effects Across Equations | 29

Predicted probabilities and differences for each model

Categorical Data Analysis

Comparing Effects Across Equations | 30

Pairwise comparison AMEs

```
est restore gsemmodel
margins, dydx(sexident sexbehav) post
qui {
mlincom 3, rowname("Het vs Bi: Ident") stat(est se p) clear
mlincom 1, rowname("Het vs Bi: Behav") stat(est se p) add
mlincom 1-3, rowname("Het vs Bi: Difference") stat(est se p) add
mlincom 2, rowname("Het vs Gay: Ident") stat(est se p) add
mlincom 2, rowname("Het vs Gay: Behav") stat(est se p) add
mlincom 2, rowname("Het vs Gay: Difference") stat(est se p) add
mlincom 1-2, rowname("Het vs Gay: Difference") stat(est se p) add
mlincom 3-4, rowname("Bi vs Gay: Ident") stat(est se p) add
mlincom (3-4)-(1-2), rowname("Bi vs Gay: Behav") stat(est se p) add
mlincom (3-4)-(1-2), rowname("Bi vs Gay: Difference") stat(est se p) add
mlincom, twidth(20) ///
title("AMEs for Sexual Orientation Within and Across Models")
```

Categorical Data Analysis

Comparing Effects Across Equations | 31

Effects of xk on different outcomes

- 1. When comparing effects on different outcome the way variables are measured must be comparable.
 - o Can you compare being ADC(married) to ADC(income)?
- 2. Two outcomes:
 - o Days of poor mental health in last month
 - o Days of poor physical health in last month

Data from the 2002, 2006, 2010, and 2014 General Social Survey

Variable	Unique	Mean	Min	Max	Label
mntlhlth	27	3.480245	0	30	days of poor mental health
physhlth	28	2.535559	0	30	days of poor physical heal
woman	2	.5132359	0	1	Woman R
married	2	.4849862	0	1	Currently Married
age	69	42.46602	18	88	age of respondent
faminc	98	39.06672	.2365	144.5027	Family Income in 1000s
race	3	1.327143	1	3	race of respondent
college	2	.3231924	0	1	R Has College Degree
parent	2	.6851047	0	1	Parent
reltrad	7	3.62663	1	7	Religious Tradition

Models: negative binomial regression

Model 1: Mental health

mntlhlth <- woman married age faminc race college parent year Model 2: Physical health

physhlth <- woman married age faminc race college parent year

Categorical Data Analysis

Comparing Effects Across Equations | 32

Categorical Data Analysis

Effects in count models

1. We use the ADC on the expected # of number of days of poor health $\Delta E(y | \mathbf{x}) / \Delta x_k = \Delta \exp(\mathbf{x}' \boldsymbol{\beta}) / \Delta x_k$

ADC on Days Reporting Poor Health

	Poor Mental Health Days	Poor Physical Health Days	Cross Model Difference
Woman	0.993***	0.773***	0.220
Married	-1.010***	-0.159	-0.851**
Parent	0.274	-0.269	0.543*
Age	-0.462***	0.491***	-0.953***
Family Income	-0.445***	-0.381***	-0.064
College	-0.879***	-0.542**	-0.337
Black vs White	-1.016***	-0.531*	-0.485
Other vs White	-0.438	0.145	-0.583
Other vs Black	0.578	0.676	-0.098
*=p= .05, **=p=.0	1, ***=p=.001	for a two-taile	d test.

Categorical Data Analysis

Comparing Effects Across Equations | 34

Results

Woman are expected to report about 0.99 more days of poor physical health per month than men and 0.77 more days of poor physical health. While the effect is 0.22 larger for mental health, the difference is not statistically significant.

Being married has a significantly larger effect on mental health than physical health. On average being married significantly reduces the days of poor mental health by 1.01 days, but the effect of marriage on physical health is nonsignificant. The effect on mental health is significantly larger $(\Delta = -.851).$

The effect of age diverge across the two outcomes, with aging associated with fewer poor mental health days but more poor physical health days

Categorical Data Analysis

Comparing Effects Across Equations | 35

Code

```
Fit models
```

```
gsem (mntlhlth <- i.woman i.married c.age faminc ///</pre>
      i.race i.college i.parent i.year, nbreg) ///
(physhlth <- i.woman i.married c.age faminc ///</pre>
                      i.race i.college i.parent i.year, nbreg), vce(robust)
est store gsemmodel
Effects for binary regressors
mlincom, clear
foreach var in woman married college parent {
    est restore gsemmodel
    margins, dydx('var') post
    qui mlincom 1, rowname(`var':MentHlth) stat(est se p) add
qui mlincom 2, rowname(`var':PhysHlth) stat(est se p) add
    qui mlincom 1-2, rowname(`var':Difference) stat(est se p) add
```

Categorical Data Analysis

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Effect of continuous regressors + SD

```
foreach var in age faminc {
        qui sum 'var' margins, at('var'=gen('var')) at('var'=gen('var' + 'r(sd)')) post qui mlincom 2-1, rowname('var':MentHlth) stat(est se p) add qui mlincom 4-3, rowname('var':PhysHlth) stat(est se p) add qui mlincom (2-1)-(4-3), rowname('var':Difference) stat(est se p) add
Effects for multicategory regressors
est restore gsemmodel
margins i.race, post
```

qui {

mlincom 2-1, rowname(blackVwhite:MentHlth) stat(est se p) add mlincom 5-4, rowname(blackVwhite:PhysHlth) stat(est se p) add mlincom (2-1)-(5-4), rowname(blackVwhite:Difference) stat(est se p) add mlincom 3-1, rowname(otherVwhite:MentHlth) stat(est se p) add
mlincom 6-4, rowname(otherVwhite:PhysHlth) stat(est se p) add
mlincom (3-1)-(6-4), rowname(otherVwhite:Difference) stat(est se p) add

mlincom 3-2, rowname(otherVblack:MentHlth) stat(est se p) add mlincom 6-5, rowname(otherVblack:PhysHlth) stat(est se p) add mlincom (3-2)-(6-5), rowname(otherVblack:Difference) stat(est se p) add

mlincom, twidth(20) /// title(AMEs for mental and physical health and cross model differences) Categorical Data Analysis

Comparing Effects Across Equations | 37

Software Implementation

- 1. To compare effects across models you need covariances across models.
- 2. Then you must jointly estimate effects across models
- 3. Stata's suest, gsem, and margins do this very generally
 - o You may have to work hard to accomplish the same thing in other packages
- 4. In Stata, **suest** is more general but post-estimation is nasty and tedious.
- 5. gsem is slow but the syntax is much simple.

Conclusions

- 1. Many of the example can be approached in other ways.
- o Our approach is not a critique of that work work
- 2. Rather we provide a general and flexible approach fully supported by mainline software
- 3. Can you think of other applications?
 - o Assessing alternative model specifications for nonlinearity?
 - o Comparing predictions for ZIP and NBRM

Categorical Data Analysis

Comparing Effects Across Equations | 38

Categorical Data Analysis

β1a Nominal outcomes

Readings and examples

Long & Freese: Chapter 8 sections on MNLM

o See references in that chapter

mdo18-nrm-*.do

Overview

- 1. What does it mean for an outcome to be nominal or ordinal?
- 2. MNLM as a set of binary logits and the IIA assumption.
- 3. Interpretation with probabilities, marginal effects, and odds ratios.
- 4. Related models.

Categorical Data Analysis

Nominal Outcomes | 1

Level of measurement

- 1. S.S. Stevens (1946) introduced the terms nominal and ordinal:
 - o Nominal scales have no ordering implied by the values
- o Ordinal scales have values indicating rank ordering on one attribute.
- 2. Debated and critiqued when proposed, his taxonomy is firmly established.

The bias-efficiency trade-off

1. The true model is:

regress y x1 x2 x3

2. Excluding variables leads to bias (if variables are correlated)

regress y x1

3. Including extra variables leads to inefficiency (larger standard errors)

regress y x1 x2 x3 x4

Categorical Data Analysis Nominal Outcomes | 2

Bias and inefficiency when assuming wrong level of measurement

		True Level			
		Nominal	Ordinal	Interval	Ratio
Assumed	N	OK	Inefficient	Inefficient	Inefficient
Level	0	Biased	OK	Inefficient	Inefficient
for	I	Biased	Biased	OK	Inefficient
Analysis	R	Biased	Biased	Biased	OK

- 1. Using MNLM with an ordinal outcome is a useful way to assess ordinality.
- $2.\,\mbox{MNLM}$ can even be used for interval outcomes to explore nonlinearities.

Categorical Data Analysis

Nominal Outcomes | 3

Binary logit with new notation

1. Linear in the logit for outcome A versus B:

$$\ln\left[\frac{\Pr(y=A\mid\mathbf{x})}{\Pr(y=B\mid\mathbf{x})}\right] = \ln\Omega(\mathbf{x}) = \beta_{0,A\mid B} + \beta_{1,A\mid B}x_1 + \beta_{2,A\mid B}x_2 + \beta_{3,A\mid B}x_3$$

2. Multiplicative in the odds:

$$\Omega(\mathbf{x}, x_2) = \exp\left[\ln\Omega(\mathbf{x}, x_2)\right]$$
$$= e^{\beta_{0,A|B}} e^{\beta_{1,A|B}x_1} e^{\beta_{2,A|B}x_2} e^{\beta_{3,A|B}x_3}$$

3. Odds ratio:

$$\frac{\Omega(\mathbf{x}, x_2 + 1)}{\Omega(\mathbf{x}, x_2)} = \frac{e^{\beta_{0,A|B}} e^{\beta_{1,A|B}x_1} e^{\beta_{2,A|B}(x_2 + 1)} e^{\beta_{3,A|B}x_3}}{e^{\beta_{0,A|B}} e^{\beta_{1,A|B}x_1} e^{\beta_{2,A|B}x_2} e^{\beta_{3,A|B}x_3}} = \exp(\beta_{2,A|B})$$

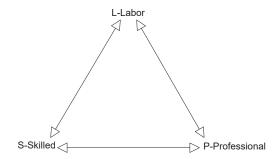
Categorical Data Analysis Nominal Outcomes | 4

Introduction to the MNLM

- 1. MNLM is equivalent to a set binary logits for all outcome pairs
 - o With three outcomes: A vs B, A vs C, B vs C
 - o Each comparison is called a contrast
- 2. Interpretation is complicated by large the number of parameters:
 - o With 5 outcomes, there are 10 binary logits
 - o With 10 outcomes, there are 45 binary logits
- 3. We start with a simple model.

MNLM with three outcomes

Categories L, S, and P with N_L , N_S , and N_P observations.



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MNLM is a set of BLM that are simultaneously estimated.

L vs S

$$\ln\left[\frac{\Pr(L \mid Ed)}{\Pr(S \mid Ed)}\right] = \beta_{0,L \mid S} + \beta_{1,L \mid S} Ed$$

S vs P

$$\ln \left[\frac{\Pr(S \mid Educ)}{\Pr(P \mid Educ)} \right] = \beta_{0,S\mid P} + \beta_{1,S\mid P} Ed$$

I vs F

$$\ln \left[\frac{\Pr(L \mid Educ)}{\Pr(P \mid Educ)} \right] = \beta_{0,L\mid P} + \beta_{1,L\mid P} Ed$$

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Redundancy among the BLMs

1. Logit for L vs P

$$\ln \left[\frac{\Pr(L \mid Ed)}{\Pr(P \mid Ed)} \right] = \ln \Pr(L \mid Ed) - \ln \Pr(P \mid Ed) + 0$$

2. Adding $0 = \ln \Pr(S \mid Ed) - \ln \Pr(S \mid Ed)$:

$$\ln\left[\frac{\Pr(L \mid Ed)}{\Pr(P \mid Ed)}\right] = \ln\Pr(L \mid Ed) - \ln\Pr(P \mid Ed) + \left[\ln\Pr(S \mid Ed) - \ln\Pr(S \mid Ed)\right] \\
= \left[\ln\Pr(L \mid Ed) - \ln\Pr(S \mid Ed)\right] + \left[\ln\Pr(S \mid Ed) - \ln\Pr(P \mid Ed)\right] \\
= \ln\left[\frac{\Pr(L \mid Ed)}{\Pr(S \mid Ed)}\right] + \ln\left[\frac{\Pr(S \mid Ed)}{\Pr(P \mid Ed)}\right]$$

Then

$$(\beta_{0,L|S} + \beta_{1,L|S}Ed) + (\beta_{0,S|P} + \beta_{1,S|P}Ed) = (\beta_{0,L|P} + \beta_{1,L|P}Ed)$$

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A minimal set of coefficients

1. Since

$$(\beta_{0,L|S} + \beta_{1,L|S}Ed) + (\beta_{0,S|P} + \beta_{1,S|P}Ed) = (\beta_{0,L|P} + \beta_{1,L|P}Ed)$$

2. From any two coefficients you can compute the third

$$\beta_{L|P} = \beta_{L|S} + \beta_{S|P}$$
$$\beta_{L|S} = \beta_{L|P} - \beta_{S|P}$$
$$\beta_{S|P} = \beta_{L|P} - \beta_{L|S}$$

3. With J outcomes, J-1 comparisons allow you to determine all contrasts o Each set of J-1 comparisons is called a <u>minimal set</u>

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Three alternative minimal sets of coefficients in 3 category MNLM

1. With base category 1:

Education	ļ.			> z		
2Skilled vs 1I 3Prof vs 1I	abor 0	.1711 2.5 .7433 8.	900 0	.004 1.	187 1	.655 .936

2. With base category 2:

Education	b	Z	P> z	e^b	e^bStdX
	+				
1Labor vs 2Skilled	-0.1711	-2.900	0.004	0.843	0.604
3Prof vs 2Skilled	0.5722	7.651	0.000	1.772	5.398

3. With base category 3:

Education	b	P> z	e^bStdX
1Labor vs	-0.7433		
2Skilled vs	-0.5722		

4. Coefficients are linked

(1L|3P) = (1L|2S) + (2S|3P)-0.74332 = -0.17109 + -0.57223

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Comparing MNLM to a set of BLMs

- 1. MNLM enforces the logical relationship among the parameters.
- 2. They do not hold exactly if you fit separate BLMs.
- 3. Consider three outcomes:

occlsp = 1 if labor, 2 if skilled, and 3 if professional; for MNLM

labrskil = 1 if labor, 0 if skilled, else missing; for BLM

profskil = 1 if professional, 0 if skilled, else missing; for BLM

labrprof = 1 if labor, 0 if professional, else missing; for BLM

4. The predictor is years of education.

Comparing BLM and MNLM estimates

Three binary logits

. logit labrskil ed

Odds of: 1Labor vs OSkilled (N=225)

labrskil | b z P>|z| e^b e^bStdX SDofX

. logit profskil ed

Odds of: 1Prof vs OSkilled (N=237)

profskil | b z P>|z| e^b e^bstdX SDofX
ed | 0.56026 7.186 0.000 1.7511 4.9101 2.8403

. logit labrprof ed

Odds of: 1Labor vs 0Prof (N=212)

| labrprof | b | z | P > | z | e^b | e^b | stdX | SDofX | SDofX | ed | -0.69037 | -7.115 | 0.000 | 0.5014 | 0.1065 | 3.2443

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One MNLM

. mlogit occlsp ed

mlogit (N=337): Factor Change in the Odds of occlsp

Variable: ed (sd=2.9464271)

Odds comparing Alternative 1 to Alternative 2	b	z	P> z
1Labor vs 2Skilled	-0.1711	-2.900	0.004
1Labor vs 3Prof	-0.7433	-8.773	0.000
3Prof vs 2Skilled	0.5722	7.651	0.000

Compared to the BLM results

	b	z	P> z
	-0.1840	-2.989	0.003
	-0.6904	-7.115	0.000
	0.5603	7.186	0.000

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Independence of irrelevant alternatives (IIA)

- 1. MNLM assumes that when a person chooses between choice J and choice K, the decision is not affect by other choices that are available.
- o This is the IIA assumption
- o It is why BLM can be used to estimate MNLM parameters
- 2. The assumption is fundamental to the model
- 3. Is it a weakness or a strength?
- o Opionions vary
- 4. Can you test the assumption?
 - Not really
- 5. What do you do?
 - o Have choices that are distinct, nonreduncant alternatives
- 6. Details follow

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Why IIA would fail: McFadden's buses

- 1. A person has two choices: Pr(car) = 1/2 and Pr(red bus) = 1/2
- 2. The odds of taking a car versus a red bus:

$$\frac{\Pr(\operatorname{car})}{\Pr(\operatorname{red} \operatorname{bus})} = \frac{1/2}{1/2} = 1$$

- 3. A new bus company opens with identical service using blue buses.
- 4. IIA requires:

$$Pr(car) = 1/3$$
; $Pr(red bus) = 1/3$; $Pr(blue bus) = 1/3$

5. This maintains the odds of one

$$\frac{\Pr(\text{car})}{\Pr(\text{red bus})} = 1 = \frac{1/3}{1/3}$$

6. Substantively, we would expect a violation of IIA:

$$Pr(car) = 1/2;$$
 $Pr(red bus) = 1/4;$ $Pr(blue bus) = 1/4$

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Does IIA make sense?

- 1. IIA requires that if a new choice becomes available, probabilities for prior choices adjust precisely to retain the original odds among choices
- 2. McFadden suggested that IIA implies that MNLM should only be used when:

Outcome categories can plausibly be assumed to be distinct and weighed independently in the eyes of each decision maker

3. Amemiya suggested that the MNLM works well when:

The alternatives are dissimilar

4. Specifying a model with distinct outcomes that are not substitutes for one another is reasonable, albeit ambiguous, advice.

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Formal tests of IIA

- 1. Reviewers sometimes demand an IIA test.
 - o Simulations by Cheng and Long (SMR) and other studies found that formal tests do not work well
- 2. Hausman and McFadden proposed a Hausman-type test of IIA
 - o This compares two estimates of the same parameters.

One estimate is consistent and efficient if the H₀ is true

The second is consistent but inefficient

- o Cheng and Long (2006) find this tests has very poor statistical properties
- 3. The Small and Hsiao (1985) LR type test
 - o The Small-Hsiao test works well sometimes
 - o Fails completely others
 - o But you can't tell when this will happen (Cheng and Long)
- 4. We found no test that works well in all cases.

Estimating MNLM with five outcomes

Descriptive statistics

occ Occupation
white Race: 1=white 0=nonwhite
ed Years of education
exper Years of work experience

-> tabulation of occ

Occupation	Freq.	Percent	Cum.
Menial BlueCol	31 69	9.20 20.47	9.20 29.67
Craft WhiteCol	84 41	24.93 12.17	54.60 66.77
Prof	112	33.23	100.00
Total	337	100.00	

. sum white ed exper

Variable	Obs	Mean	Std. Dev.	Min	Max
white	337	.9169139	.2764227	0	1
ed	337	13.09496	2.946427	3	20
exper	337	20.50148	13.95936	2	66

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Output from mlogit using base(1)

- 1. In mlogit option base(#) sets the base or reference category.
- 2. Estimates for each category compared to base category
- . mlogit occ i.white ed exper, base(1) nolog

Multinomial logistic regression				Number of obs = LR chi2(12) =			337 166.09
				Prob	> chi2	=	0.0000
Log likelihood	1 = -426.80048	3		Pseud	o R2	=	0.1629
occ	Coef.	Std. Err.	z	P> z	[95%	Conf.	Interval]
Menial	(base outco	ome)					
BlueCol							
1.white	1.236504	.7244352	1.71	0.088	1833	631	2.656371
ed	0994247	.1022812	-0.97	0.331	2998	922	.1010428
exper	.0047212	.0173984	0.27	0.786	0293	789	.0388214
_cons	.7412336	1.51954	0.49	0.626	-2.23	701	3.719477
Craft							
1.white	.4723436	.6043097	0.78	0.434	7120	817	1.656769
ed	.0938154	.097555	0.96	0.336	0973	888	.2850197
exper	.0276838	.0166737	1.66	0.097	004	996	.0603636
_cons	-1.091353	1.450218	-0.75	0.452	-3.933	728	1.751022

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WhiteCol						
1.white	1.571385	.9027216	1.74	0.082	1979166	3.340687
ed	.3531577	.1172786	3.01	0.003	.1232959	.5830194
exper	.0345959	.0188294	1.84	0.066	002309	.0715007
_cons	-6.238608	1.899094	-3.29	0.001	-9.960764	-2.516453
+ Prof						
1.white	1.774306	.7550543	2.35	0.019	.2944273	3.254186
ed	.7788519	.1146293	6.79	0.000	.5541826	1.003521
exper	.0356509	.018037	1.98	0.048	.000299	.0710028
	-11.51833	1.849356	-6.23	0.000	-15.143	-7.893659

3. A table for a paper might look like this...

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Logit Coefficients							
Comparison		Constant	WHITE	ED	EXP		
$B \mid M$	β	0.741	1.237	-0.099	0.0047		
	z	0.49	1.71	-0.97	0.27		
$C \mid M$	β	-1.091	0.472	0.094	0.027		
	z	-0.75	0.78	0.96	1.66		
$W \mid M$	β	-6.239	1.571	0.353	0.0346		
	z	-3.29	1.74	3.01	1.84		
$P \mid M$	β	-11.518	1.774	0.779	0.0357		
	z	-6.23	2.35	6.79	1.98		

4. This table corresponds to these equations

$$\ln \Omega_{B|M}(\mathbf{x}_i) = \beta_{0,B|M} + \beta_{1,B|M} WHITE + \beta_{2,B|M} ED + \beta_{3,B|M} EXP$$

$$\ln \Omega_{C|M}(\mathbf{x}_i) = \beta_{0,C|M} + \beta_{1,C|M}WHITE + \beta_{2,C|M}ED + \beta_{3,C|M}EXP$$

$$\ln \Omega_{W|M}(\mathbf{x}_i) = \beta_{0,W|M} + \beta_{1,W|M} WHITE + \beta_{2,W|M} ED + \beta_{3,W|M} EXP$$
...

$$\ln \Omega_{P|M}(\mathbf{x}_i) = \beta_{0,P|M} + \beta_{1,P|M}WHITE + \beta_{2,P|M}ED + \beta_{3,P|M}EXP$$

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Should you rely on a minimal set?

These are minimal sets of coefficients for education

Base BlueCol: 0 significant coefficients

			e^b	P> z
WhiteCol	vs	BlueCol	1.3978	0.720
Prof	vs	BlueCol	1.7122	0.501
Craft	vs	BlueCol	0.4657	0.227
Menial	vs	BlueCol	0.2904	0.088

Base WhiteCol: 0 significant coefficients

			e^b	P> z
Prof	vs	WhiteCol	1.2250	0.815
BlueCol	vs	WhiteCol	0.7154	0.720
Craft	vs	WhiteCol	0.3332	0.179
Monial	770	WhiteCol	0 2078	0 082

Base Craft: 1 significant coefficient

			e^b	P> z
BlueCol	vs	Craft	2.1472	0.227
WhiteCol	vs	Craft	3.0013	0.179
Prof	vs	Craft	3.6765	0.044
Menial	vs	Craft	0.6235	0.434

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Base Menial: 1 significant coefficient

			e^b	P> z
Craft	vs	Menial	1.6037	0.434
BlueCol	vs	Menial	3.4436	0.088
WhiteCol	vs	Menial	4.8133	0.082
Prof	vs	Menial	5.8962	0.019

Base Prof: 2 significant coefficients

			e^b	P> z
WhiteCol	vs	Prof	0.8163	0.815
BlueCol	vs	Prof	0.5840	0.501
Craft	vs	Prof	0.2720	0.044
Menial	vs	Prof	0.1696	0.019

- 1. You should not use a minimal set to evaluate the overall significance of x_k
- 2. This is why minimal sets can be misleading

Graphs with different base categories

M C B WP

-2 -1.33 -67 0 67 1.33 2
Logit Coefficient Scale Relative to Category Menial

M C B WP

-2 -1.33 -67 0 67 1.33 2
Logit Coefficient Scale Relative to Category BlueCol

M C B WP

-2 -1.33 -67 0 67 1.33 2
Logit Coefficient Scale Relative to Category WhiteCol

M C B WP

-2 -1.33 -67 0 67 1.33 2
Logit Coefficient Scale Relative to Category WhiteCol

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Looking at all ORs is overwhelming....

mlogit (N=337): Factor change in the odds of occ

Variable: 1.white (sd=0.276)

		b	z	P> z	e^b	e^bStd1
Menial	vs BlueCol	-1.2365	-1.707	0.088	0.290	0.710
Menial	vs Craft	-0.4723	-0.782	0.434	0.624	0.878
Menial	vs WhiteCol	-1.5714	-1.741	0.082	0.208	0.648
Menial	vs Prof	-1.7743	-2.350	0.019	0.170	0.612
BlueCol	vs Menial	1.2365	1.707	0.088	3.444	1.40
BlueCol	vs Craft	0.7642	1.208	0.227	2.147	1.235
BlueCol	vs WhiteCol	-0.3349	-0.359	0.720	0.715	0.912
BlueCol	vs Prof	-0.5378	-0.673	0.501	0.584	0.86
Craft	vs Menial	0.4723	0.782	0.434	1.604	1.13
Craft	vs BlueCol	-0.7642	-1.208	0.227	0.466	0.81
Craft	vs WhiteCol	-1.0990	-1.343	0.179	0.333	0.73
Craft	vs Prof	-1.3020	-2.011	0.044	0.272	0.69
WhiteCol	vs Menial	1.5714	1.741	0.082	4.813	1.54
WhiteCol	vs BlueCol	0.3349	0.359	0.720	1.398	1.09
WhiteCol	vs Craft	1.0990	1.343	0.179	3.001	1.35
WhiteCol	vs Prof	-0.2029	-0.233	0.815	0.816	0.94
Prof	vs Menial	1.7743	2.350	0.019	5.896	1.63
Prof	vs BlueCol	0.5378	0.673	0.501	1.712	1.16
Prof	vs Craft	1.3020	2.011	0.044	3.677	1.43
Prof	vs WhiteCol	0.2029	0.233	0.815	1.225	1.05

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Variable: ed (sd=2.946)

		b	z	P> z	e^b	e^bStdX
Menial	vs BlueCol	0.0994	0.972	0.331	1.105	1.340
Menial	vs Craft	-0.0938	-0.962	0.336	0.910	0.758
Menial	vs WhiteCol	-0.3532	-3.011	0.003	0.702	0.353
Menial	vs Prof	-0.7789	-6.795	0.000	0.459	0.101
BlueCol	vs Menial	-0.0994	-0.972	0.331	0.905	0.746
BlueCol	vs Craft	-0.1932	-2.494	0.013	0.824	0.566
BlueCol	vs WhiteCol	-0.4526	-4.425	0.000	0.636	0.264
BlueCol	vs Prof	-0.8783	-8.735	0.000	0.415	0.075
Craft	vs Menial	0.0938	0.962	0.336	1.098	1.318
Craft	vs BlueCol	0.1932	2.494	0.013	1.213	1.767
Craft	vs WhiteCol	-0.2593	-2.773	0.006	0.772	0.466
Craft	vs Prof	-0.6850	-7.671	0.000	0.504	0.133
WhiteCol	vs Menial	0.3532	3.011	0.003	1.424	2.831
WhiteCol	vs BlueCol	0.4526	4.425	0.000	1.572	3.794
WhiteCol	vs Craft	0.2593	2.773	0.006	1.296	2.147
WhiteCol	vs Prof	-0.4257	-4.616	0.000	0.653	0.285
Prof	vs Menial	0.7789	6.795	0.000	2.179	9.923
Prof	vs BlueCol	0.8783	8.735	0.000	2.407	13.300
Prof	vs Craft	0.6850	7.671	0.000	1.984	7.526
Prof	vs WhiteCol	0.4257	4.616	0.000	1.531	3.505

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Variable: 6	exper (s	d=13.959)
-------------	----------	-----------

		l b	z	P> z	e^b e	e^bStdX
Menial	vs BlueCol	-0.0047	-0.271	0.786	0.995	0.936
Menial	vs Craft	-0.0277	-1.660	0.097	0.973	0.679
Menial	vs WhiteCol	-0.0346	-1.837	0.066	0.966	0.617
Menial	vs Prof	-0.0357	-1.977	0.048	0.965	0.608
BlueCol	vs Menial	0.0047	0.271	0.786	1.005	1.068
BlueCol	vs Craft	-0.0230	-1.829	0.067	0.977	0.726
BlueCol	vs WhiteCol	-0.0299	-1.954	0.051	0.971	0.659
BlueCol	vs Prof	-0.0309	-2.147	0.032	0.970	0.649
Craft	vs Menial	0.0277	1.660	0.097	1.028	1.472
Craft	vs BlueCol	0.0230	1.829	0.067	1.023	1.378
Craft	vs WhiteCol	-0.0069	-0.495	0.621	0.993	0.908
Craft	vs Prof	-0.0080	-0.627	0.531	0.992	0.895
WhiteCol	vs Menial	0.0346	1.837	0.066	1.035	1.621
WhiteCol	vs BlueCol	0.0299	1.954	0.051	1.030	1.517
WhiteCol	vs Craft	0.0069	0.495	0.621	1.007	1.101
WhiteCol	vs Prof	-0.0011	-0.07	3 0.94	11 0.9	99 0.9
Prof	vs Menial	0.0357	1.977	0.048	1.036	1.645
Prof	vs BlueCol	0.0309	2.147	0.032	1.031	1.540
Prof	vs Craft	0.0080	0.627	0.531	1.008	1.118
Prof	vs WhiteCol	0.0011	0.073	0.941	1.001	1.015

Our task is to make sense out of all of these numbers

Categorical Data Analysis

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Roadmap

- 1. MNLM as a probability model.
- 2. Fitting the model with MLE.
- 3. Omnibus test of a regressor.
- 4. Tests if categories can be combined.
- 5. Interpretation
- o Probabilities
- o Marginal effects
- o Odds ratios with reservations

Categorical Data Analysis Nominal Outcomes | 28

MNLM as a Probability Model

1. We can solve the J-1 equations for $\log \left[\Pr(y_i = m \mid \mathbf{x}_i) / \Pr(y_i = B \mid \mathbf{x}_i) \right]$:

$$\Pr\left(y_i = m \mid \mathbf{x}_i\right) = \frac{\exp\left(\mathbf{x}_i \mathbf{\beta}_{m|J}\right)}{\sum_{j=1}^{J} \exp\left(\mathbf{x}_i \mathbf{\beta}_{j|J}\right)}$$

2. You get the same values regardless of the base J you use.

ML estimation

- 1. $Pr(y=m \mid x_i)$ is the probability of observing outcome m for person i:
 - o If person i choses outcome j, then $p_i = Pr(y=j|x_i)$
- 2. If observations are independent, the likelihood equation is:

$$L(\boldsymbol{\beta}_{2|J},...,\boldsymbol{\beta}_{J|J} | \mathbf{y}, \mathbf{X}) = \prod_{i=1}^{N} p_i$$

3. Solving for the parameters works well even with small samples.

Test that a variable has no effect

1. The hypothesis that x_k has no effect involves J-1 coefficients:

$$H_0: \beta_{k,B|M} = \beta_{k,C|M} = \beta_{k,W|M} = \beta_{k,P|M} = 0$$

2. This is <u>not</u> equivalent to combined tests of individual coefficients

$$H_0: \beta_{k,B|M} = 0$$
 $H_0: \beta_{k,C|M} = 0$ $H_0: \beta_{k,W|M} = 0$ $H_0: \beta_{k,P|M} = 0$

3. As with BRM, testing βs does not replace tests of marginal effects $% \beta s$

Wald test that all coefficients for x_k are 0:

$$W_k = \hat{\boldsymbol{\beta}}_k' Var(\hat{\boldsymbol{\beta}}_k)^{-1} \hat{\boldsymbol{\beta}}_k$$
 where $W_k \sim \chi_{J-1}^2$ if H_0 is true

LR test that all coefficients for xk are 0: s

- 1. Estimate $G_{ ext{Full}}^2$ for full model, and $G_{ ext{Restricted}}^2$ for $M_{ ext{Restricted}}$ by excluding x_k
- 2. $\emph{M}_{\text{Restricted}}$ has $\emph{J}-1$ fewer parameters. The LR test is

$$G_{\text{Restricted Full}}^2 = G_{\text{Full}}^2 - G_{\text{Restricted}}^2 \sim \chi_{J-1}^2$$
 if H₀ is true.

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Categorical Data Analysis

Wald tests using mlogtest

. mlogtest, wald

Wald tests for independent variables (N=337)

Ho: All coefficients associated with given variable(s) are 0

	chi2	df	P>chi2
	+		
1.white	8.149	4	0.086
ed	84.968	4	0.000
exper	7.995	4	0.092

The effect of race is not significant at the .05 level (G2=8.15, df=4).

The effect of education is significant at the .01 level.

The effect of experience is significant at the .10 level but not at the .05 level

Categorical Data Analysis

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Wald test of regression coefficients using test

. test 1.white $\ensuremath{//}$ test will work with svy estimates too

 \leftarrow This is $\beta_{\text{white},M|M}$

- . * 1.white is the variable created from i.white!
- (1) [Menial]o.white = 0
 (2) [BlueCol]white = 0
- (3) [Craft]white = 0
- (4) [WhiteCol]white = 0
- (5) [Prof]white = 0
 Constraint 1 dropped

- . test ed
- <snip>
- . test exper
 <snip?</pre>

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LR test using mlogtest

. estimates restore full
(results full are active now)

. mlogtest, lr

Likelihood-ratio tests for independent variables (N=337)

	chi2	df	P>chi2
1.white	8.095	4	0.088
ed	156.937	4	0.000
exper	8.561	4	0.073

LR tests using Irtest

- . quietly mlogit occ white ed exper, base(1) // full model
- estimates store full
- . quietly mlogit occ ed exper, base(1) $\ensuremath{//}$ restricted model
- . estimates store dropwhite
- . lrtest full dropwhite

Likelihood-ratio test	LR chi2(4) = 8.10
(Assumption: dropwhite nested in full	l) Prob > chi2 = 0.0881

Categorical Data Analysis

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Test if outcomes can be combined

1. If all $\beta_{k,P|W}$ are 0, then P and W are indistinguishable.

$$H_0: \beta_{1,P|W} = \beta_{2,P|W} = \beta_{3,P|W} = 0$$

- 2. Why test if outcomes can be combined?
- 3. Substantively
 - You want to know if professional and white collar jobs are differentiated by the predictors in the model
- 4. To simplify the model
 - $\,\circ\,$ You have a five point scale of party and want to combine

Strong Democrat and Democrat

Strong Republican and Republican

5. Decisions to combine categories must be made sequentially as now shown.

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Tests for combining can lead to inconsistencies

- 1. Tests of hypothesis are not algebraic statements.
- 1. A test for combining M and B is not significant (p=.251)

M can be combined with B M = B

2. A test for combining M and C is not significant (p=.337)

M can be combined with C M = C

- 3. If $\underline{M} = \underline{B}$ and $\underline{M} = \underline{C}$, then algebraically $\underline{B} = \underline{C}$
- 4. Yet a test for combining B and C is significant (p=.003)

B cannot be combined with C $B \neq C$

- 5. If you decide to combine categories based on testing
 - o Combine only two categories for a set of tests
 - o Fit the model with the new set of outcomes
 - o Test for indistinguishability in the new model

Wald tests for combining outcomes

. mlogtest, combine

Wald tests for combining alternatives (N=337)

Ho: All coefficients except intercepts associated with a given pair of alternatives are 0 (i.e., alternatives can be combined)

chi2	df	P>chi2
3.994	3	0.262
3.203	3	0.361
11.951	3	0.008
48.190	3	0.000
8.441	3	0.038
20.055	3	0.000
76.393	3	0.000
8.892	3	0.031
60.583	3	0.000
22.203	3	0.000
	3.994 3.203 11.951 48.190 8.441 20.055 76.393 8.892 60.583	3.994 3 3.203 3 11.951 3 48.190 3 8.441 3 20.055 3 76.393 3 8.892 3 60.583 3

Or use mlogtest, lrcomb for LR tests

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Specification searches

- 1. Tests for combining categories and tests that all coefficients for a variable are zero can be used in a specification search.
- 2. Think substantively about changes to your model.
 - o Do not to over-fit your data
 - o Examine individual coefficients before revising your model
- In models obtained from tests using the same data, significance levels are invalid.
 - Consider randomly dividing the sample into an <u>exploration sample</u> and a verification sample

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Overview of interpretation

- 1. The MNLM has many parameters.
- 2. Do not:
 - o Look only at a minimal set of parameters
 - o Discuss only the stars and signs of coefficients
- 3. Interpretation should include
 - o Predicted probabilities
 - o Marginal effects
 - o Odds ratios
- 4. Only some methods are shown in this lecture
 - \circ Methods from the ordinal lecture that do not depend on the ordinality can be used for nominal outcomes

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Example: Attitudes toward working mothers

Outcome

Working mothers can have a warm relationship with their children?

1. Responses in variable warm are

<u> </u>	Freq.	Percent
1 Strongly Disagree 2 Disagree 3 Agree 4 Strongly agree	297 723 856 417	12.95 31.53 37.33 18.19
Total	2,293	100.00

2. Remember:

Agree: support for working mothers

Disagree: lack of support for working moms

Categorical Data Analysis Nominal Outcomes | 39

Regressors

. codebook yr89 male white age prst, compact

Vari	able Obs	Unique	Mean	Min	Max	Label
yr89	2293	2	.3986044	0	1	Survey year: 1=1989 0=1977
male	2293	2	.4648932	0	1	Gender: 1=male 0=female
whit	e 2293	2	.8765809	0	1	Race: 1=white 0=not white
age	2293	72	44.93546	18	89	Age in years
prst	2293	58	39.58526	12	82	Occupational prestige

. tab edcat

Years of education in groups	Freq.	Percent	Cum.
0-11 yrs 12 yrs 13-15 yrs 16-20 yrs	670 782 449 392	29.22 34.10 19.58 17.10	29.22 63.32 82.90 100.00
Total	2,293	100.00	

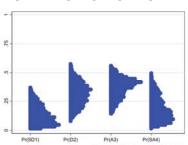
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Fitting the model

1. Treating warm as nominal and fit the model mlogit warm i.yr89 i.male i.white age i.edcat prst, base(1)

Predictions

I start by looking for anomalies and outliers in the predictions and find none. predict SDpr1 Dpr2 Apr3 SApr4



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Average marginal effects -- we need a plot!

- 1. ADC(x_k) is the counterpart to $\beta_k s$ in LRM
- 2. It produces too much information to easily absorb
- . mchange, amount(one sd) // no marginal changes

mlogit: Changes in Pr(y) | Number of obs = 2293

Expression: Pr(warm), predict(outcome())

1	1 SD	2 D	3 A	4 SA
yr89				
1989 vs 1977	-0.095	-0.029	0.079	0.045
p-value	0.000	0.136	0.000	0.006
male				
Male vs Female	0.038	0.120	-0.010	-0.148
p-value	0.006	0.000	0.622	0.000
white				
White vs NonWhite	0.040	0.018	-0.006	-0.052
p-value	0.036	0.529	0.838	0.038
::				

On average being male decrease the probability of strong support for working mothers by .15 (p<.001).

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!	1 SD	2 D	3 A	4 SA
age				
+1	0.002	0.004	-0.003	-0.003
p-value	0.000	0.000	0.000	0.000
+SD	0.037	0.059	-0.054	-0.042
p-value	0.000	0.000	0.000	0.000
edcat				
12 yrs vs 0-11 yrs	-0.012	-0.004	0.028	-0.012
p-value	0.535	0.880	0.305	0.580
13-15 yrs vs 0-11 yrs	-0.056	-0.042	0.053	0.045
p-value	0.013	0.171	0.104	0.084
16-20 yrs vs 0-11 yrs	-0.090	-0.015	0.050	0.055
p-value	0.000	0.694	0.198	0.093
13-15 yrs vs 12 yrs	-0.044	-0.038	0.025	0.057
p-value	0.029	0.167	0.380	0.011
16-20 yrs vs 12 yrs	-0.078	-0.011	0.022	0.066
p-value	0.000	0.745	0.510	0.017
16-20 yrs vs 13-15 yrs	-0.034	0.028	-0.003	0.009
p-value	0.096	0.415	0.934	0.746
prst				
+1	0.000	-0.002	0.001	0.001
p-value	0.818	0.011	0.193	0.220
+SD	0.002	-0.029	0.016	0.012
p-value	0.841	0.009	0.214	0.240

Let's plot the effects.

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Average marginal effects: two critical variables

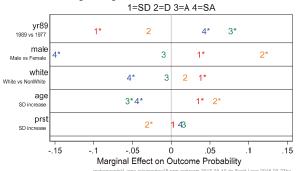
Average marginal effect 1=SD 2=D 3=A 4=SA yr89 1989 vs 1977 male Male vs Female 4* 3 1* 2* -.15 -.1 -.05 0 .05 .1 .15 Marginal Effect on Outcome Probability mechaneselells are classpared 18-mm ordwarm 2017-03-10 do Scott Long 2018-03-27 he mechaneselells are confidenced file-mm-ordwarm 2017-03-10 do Scott Long 2018-03-27 he

Men are more likely to have negative attitudes toward working women than are women. On average men are .15 less likely (p<.01) to strongly support working women and .12 more likely (p<.01) to be negative. From 1977 to 1989 attitudes have become more positive, with significant increases of .05 in strong support and .08 in support, with a decrease of .10 in the most negative attitudes.

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Average marginal effects of continuous and binary regressors



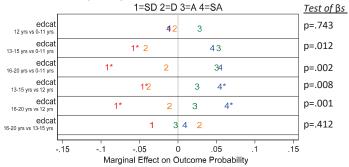


- 1. Why are the colors ordered red orange green blue used?
- 2. Is this consistent with warm being ordinal?

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Average marginal effects of education

Average marginal effect



- 1. Compare ME's to test all β s are 0.
- 2. Effects vary by outcome and contrasts.

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Code for mchangeplot

1. After running mchange, create a quick graph mchangeplot

2. Create a customized graph:

mchangeplot yr89 male white age prst, /// regressors to plot
 min(-.15) max(.15) gap(.05) /// tick marks on axis
 mcol(red orange green blue) /// colors of symbols
 title(Average marginal effect, position(11)) ///
 subtitle(1=SD 2=D 3=A 4=SA) ///
 sig(.05) /// add * if sig at .05 level
 aspect(.5) leftmargin(10) // tweak shape of graph

Tests of regressors

- We can test that the 4 coefficients for each regressor are simultaneously 0.
 2.edcat, 3.edcat, and 4.edcat are contrasts with 1.edcat
- . mlogtest, wald

Ho: All coefficients associated with given variable(s) are $\mathbf{0}$

	chi2	df	P>chi2	
1.yr89	54.503	3	0.000	
1.male	100.836	3	0.000	
1.white	7.638	3	0.054	
age	86.556	3	0.000	
2.edcat	1.241	3	0.743	<= 12 vs 0-13
3.edcat	10.994	3	0.012	<= 13-15 vs 0-13
4.edcat	15.119	3	0.002	<= 16-20 vs 0-13
prst	6 901	3	0.075	

The effect of gender is significant (X2=100.8, df=3, p<.001).

Prestige does not significantly affect attitudes toward working women.

2.1 ignore these and focus on marginal effects.

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Tests for combining categories

- 1. To simplify analysis, I consider dichotomizing into positive vs negative attitudes.
- . mlogtest, combine

Wald tests for combining alternatives (N=2293)

Ho: All coefficients except intercepts associated with a given pair of alternatives are 0 (i.e., alternatives can be combined)

	chi2	df	P>chi2
1 SD & 2 D	38.245	8	0.000
1_SD & 3_A	134.132	8	0.000
1_SD & 4_SA	185.858	8	0.000
2_D & 3_A	95.727	8	0.000
2_D & 4_SA	172.166	8	0.000
3_A & 4_SA	53.660	8	0.000

2. The evidence does not support combining categories.

Categorical Data Analysis

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Example: Political orientation

- 1. 1992 American National Election Study
- 2.1 was given this data as an example for ordinal logit.

Outcome: party affiliation

. use partyid4, clear (partyid4.dta | 1992 American National Election Study | 2014-03-12)

. tab party, miss

	Party ID	Freq.	Percent	Cum.
D	StrDem	266	19.25	19.25
d	Dem	427	30.90	50.14
i	Indep	151	10.93	61.07
r	Rep	369	26.70	87.77
R	StrRep	169	12.23	100.00
	Total	1,382	100.00	

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Regressors

party Party ID age Age

income Income in \$1,000s

black Black? female Female?

Level of education versus "not hs grad" educ

. sum party age income black female i.educ

Variable	Obs	Mean	Std. Dev.	Min	Max
party	1382	2.817656	1.342787	1	5
age	1382	45.94645	16.78311	18	91
income	1382	37.45767	27.78148	1.5	131.25
black	1382	.1374819	.34448	0	1
female	1382	.4934877	.5001386	0	1
educ					
hs only	1382	.5803184	.4936854	0	1
college	1382	.2590449	.4382689	0	1

[&]quot;10" versions of variables divide age and income by 10.

Categorical Data Analysis

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Fit MNLM and test regressors

- . mlogit party age10 income10 i.black i.female i.educ
- . mlogtest, lr set(educ_set=1.highschool 1.college)

LR tests for independent variables (N=1382)

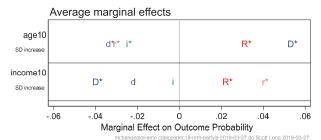
Ho: All coefficients associated with given variable(s) are 0

	chi2	df	P>chi2
	+		
age10	45.165	4	0.000
income10	24.361	4	0.000
1.black	126.467	4	0.000
1.female	9.143	4	0.058
1.highschool	5.567	4	0.234
1.college	21.582	4	0.000
educ_set	26.881	8	0.001

educ_set contains: 1.highschool 1.college

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Average marginal effects (AME)



Age increases the probability of the extreme affiliations and decreases the probability of less extreme affiliations.

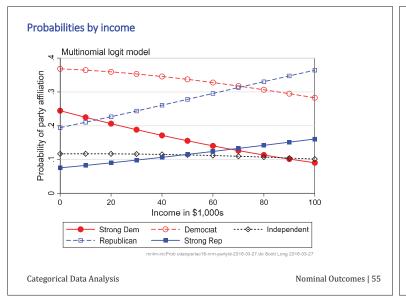
Income increase Republican affiliations, while decreasing Democratic affiliations.

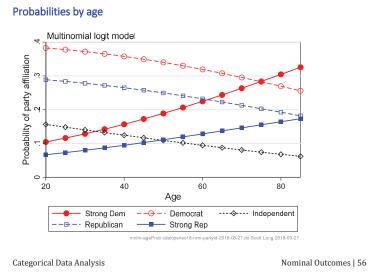
Categorical Data Analysis Nominal Outcomes | 53

Plots of probabilities

- 1. For continuous regressors, plots can be useful.
- 2. One variable changes while others are constant.
 - o Unless variables are linked, like age and age-squared
- 3. I create two plots:
- o Age changes while holding other variables at their means
- o Income changes holding other variables at their means
- 4. The probability lines are nearly straight so that the AMEs or DCMs would be good summaries.
 - o The only way to know if a plot is useful is to create it

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Commands for plots

Generate variables to plot

mgen, atmeans at(age10=(2(.5)8.5)) stub(MNLMage)

Predictions from: margins, atmeans at(age10=(2(.5)8.5)) predict(outcome(5))

Variable	Obs	Unique	Mean	Min	Max	Label
MNLMagepr1	14	14	.2046258	.1047786	.3256354	pr(y=SD) from margins
MNLMagell1	14	14	.1675598	.0768825	.2487619	95% lower limit
MNLMageul1	14	14	.2416917	.1326748	.4025089	95% upper limit
MNLMageage10	14	14	5.25	2	8.5	Age in decades
MNLMageCpr1	14	14	.2046258	.1047786	.3256354	pr(y<=SD)
MNLMagepr2	14	14	.329003	.2561781	.3826132	pr(y=D) from margins
MNLMagel12	14	14	.2874055	.1949605	.3331204	95% lower limit
MNLMageul2	14	14	.3706006	.3173957	.435444	95% upper limit
MNLMageCpr2 <snip></snip>	14	14	.5336288	.4873918	.5818136	pr(y<=D)

Specified values of covariates

	1.	1.	2.	3.
income10	black	female	educ	educ
3.745767	.1374819	.4934877	.5803184	.2590449

mgen, atmeans at(income10=(0(1)10)) stub(MNLMinc)

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```
Customize variables and options for plots
gen PLTincome = MNLMincincome10*10
label var PLTincome "Income in $1,000s"
gen PLTage = MNLMageage10*10
gen Finage - mammageageactors label var PITage "Age" local yaxis p "ytitle(Probability of party affiliation)" local yaxis p "'yaxis p' ylab(0(.1).4, grid) ylin(0 .4, lcol(gsl4))" local yaxis c ///
     "ytitle(Cumulative probability) ylab(0(.2)1, grid) ylin(0 1, lcol(gs14))"
local titleopt "position(11) size(medium)"
* line options for probabilities
local line5_opts "msym(0 Oh dh sh s)"
local line5_opts "line5_opts' lwid(*1.3 *1.3 *1.3 *1.3 *1.3)"
local line5_opts "line5_opts' lapt(solid dash shortdash dash solid)"
local line5_opts "line5_opts' mcol(red red*.8 black blue*.8 blue)"
local line5_opts "`line5_opts' lcol(red red*.8 black blue*.8 blue)"
label var MNLMageprl "Strong Dem"
label var MNLMagepr2 "Democrat"
label var MNLMagepr3 "Independent"
label var MNLMagepr4 "Republican"
label var MNLMagepr5 "Strong Rep"
label var MNLMincpr1 "Strong Dem"
label var MNLMincpr3 "Independent"
label var MNLMincpr3 "Independent"
label var MNLMincpr4 "Republican"
label var MNLMincpr5 "Strong Rep"
```

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Create plots

```
probability by age
graph twoway (connected MNLMagepr1 MNLMagepr2 MNLMagepr3 ///
MNLMagepr4 MNLMagepr5 PLTage, `line5_opts'), ///
title("'title'", `titleopt') `yaxis_p' `xaxis_age' ///
        legend(rows(2))
  probability by income
```

graph twoway (connected MNLMincpr1 MNLMincpr2 MNLMincpr3 /// MNLMincpr4 MNLMincpr5 PLTincome, `line5_opts'), ///
title("`title'", `titleopt') `yaxis_p' `xaxis_inc' /// legend(rows(2))

See Long and Freese for lots of details!

Test IIA with a Hausman test

- 1. If IIA holds, the coefficient from binary logit:
- . gen party15 = 1 if party==1
 . replace party15 = 0 if party==5
- . logit party15 age, nolog

Categorical Data Analysis

party15 | Coef. Std. Err. P> | z | [95% Conf. Interval] age | .0102276 .005633 -.0008129 1.82 0.069

2. Should be close to those from the MNLM:

. mlogit party age, base(5)

party | Coef. Std. Err. $z \qquad P > |z|$ [95% Conf. Interval] StrDem .0104532 .0056788 1.84 0.066 -.0006771 .0215834 _____ (base outcome) ----

3. IIA tests formally assess coefficients from alternative specifications

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Hausman test

. mlogtest, hausman

Hausman tests of IIA assumption (N=1382)

Ho: Odds(Outcome-J vs Outcome-K) are independent of other alternatives

	chi2	df	P>chi2
	+		
StrDem	4.622	20	1.000
Dem	0.919	21	1.000
Indep	-2.244	19	
Rep	3.030	21	1.000
StrRep	-0.580	21	

Note: A significant test is evidence against Ho.

- 1. The Hausman test often produces negative chi-squares.
- 2. In simulations, its size properties are very bad.

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Small-Hsiao

Randomly divides the samples and compares estimates (roughly speaking)
 Random numbers are used to divide the sample

Small-Hsiao: Seed 124386

- 1. It appears that IIA is supported
- . mlogtest, smhsiao

Small-Hsiao tests of IIA assumption (N=1382)

Ho: Odds(Outcome-J vs Outcome-K) are independent of other alternatives

P>chi2	df	chi2	lnL(omit)	lnL(full)	
0.934	21	12.198	-690.654	-696.753	StrDem
0.760	21	16.166	-557.488	-565.571	Dem
0.924	21	12.547	-758.290	-764.563	Indep
0.936	21	12.140	-615.492	-621.562	Rep
0.675	21	17.587	-752.804	-761.598	StrRep

Note: A significant test is evidence against Ho.

Categorical Data Analysis Nominal Outcomes | 62

Seed 254331

- 1. It appears IIA is not supported
- . mlogtest, smhsiao

Small-Hsiao tests of IIA assumption (N=1382)

Ho: Odds(Outcome-J vs Outcome-K) are independent of other alternatives

	lnL(full)	lnL(omit)	chi2	df	P>chi2
StrDem	-727.367	-692.048	70.639	21	0.000
Dem	-610.636	-573.268	74.736	21	0.000
Indep	-783.456	-747.654	71.604	21	0.000
Rep	-650.962	-615.434	71.057	21	0.000
StrRep	-751.887	-740.193	23.388	21	0.324

Note: A significant test is evidence against Ho.

* Odds ratio plots

The additive links among parameters

1. Because of IIA:

$$\ln\left[\frac{\Pr(L \mid Ed)}{\Pr(P \mid Ed)}\right] = \ln\left[\frac{\Pr(L \mid Ed)}{\Pr(S \mid Ed)}\right] + \ln\left[\frac{\Pr(S \mid Ed)}{\Pr(P \mid Ed)}\right]$$

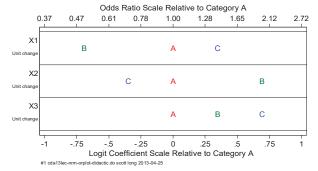
- 2. So that $\beta_{L|P} = \beta_{L|S} + \beta_{S|P}$
- 3. Knowing the minimal set we can determine all other parameters.
- 4. We can plot them just like stops on a subway line.

Categorical Data Analysis Nominal Outcomes | 64

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Odds ratio plot



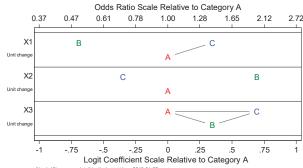
1. Distance: B -> A = .693

2. Distance: A -> C = .347

3. Distance: B -> C = 1.040 = .693 + .347

Categorical Data Analysis Nominal Outcomes | 65

A line indicates a non-significant coefficient



#1 cda13lec-nrm-orplot-didactic.do scott long 2013-04-29

Categorical Data Analysis

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MNLM for occupation

Outcomes

M == menial job
B == blue collar job
C == craft job
W == white collar job
P == professional job

Regressors

white == white = 1, vs nonwhite
ed == years of education
exper == years of work experience

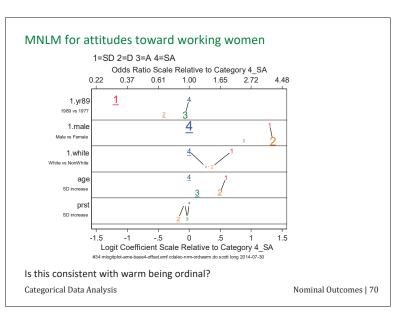
Categorical Data Analysis

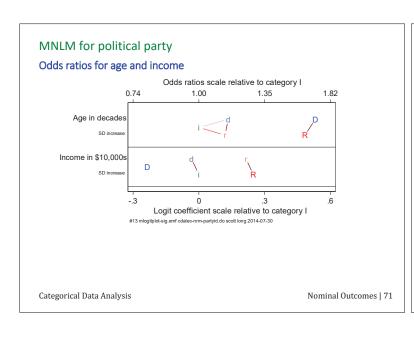
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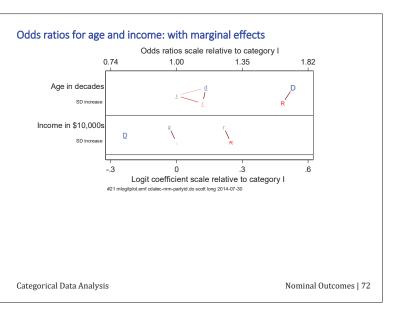
Odds ratio plot Odds Ratio Scale Relative to Category Prof 0.08 0.14 0.22 0.37 0.61 1.00 1.65 1.white ed W SD increas expe SD increas -2.5 -2 -1.5 -1 -.5 Logit Coefficient Scale Relative to Category Prof

Categorical Data Analysis Nominal Outcomes | 68

Size of letter proportional to size of AME Odds Ratio Scale Relative to Category Menial 0.61 1.00 1.65 2.72 4.48 12.18 1.white ed P SD inc expe Logit Coefficient Scale Relative to Category Menial Categorical Data Analysis Nominal Outcomes | 69







Review of nominal LHS

- 1. I find MNLM to be a very useful model that is easy to interpret with practice
- 2. The MNLM is a set of BLMs for all pairs of outcomes.
- 3. IIA is a restrictive assumption that does not have an adequate test.
 - o If outcomes are reasonably distinct, MNLM works well.
 - o No alternative model is available.
- MNLM can be <u>overwhelmingly complex</u> if you try to absorb all of the coefficients individually.
- 5. Plots of coefficients make it easy to uncover patterns.
 - o Use plots to find patterns to explore further
 - o DC plots are easy to explain
 - o OR plots are less effective in papers due to complexitiy in explaining them
- 6. Tables of predictions are also useful (see next lecture)

Categorical Data Analysis

β1a Ordinal outcomes

Readings and examples

Long & Freese: Chapter 7

Long, JS 2014, Regression models for nominal and ordinal outcomes pp 173-203 in H Best C Wolf Regression Analysis and Causal Inference

mdo18-orm-*.do

Nominal Outcomes L 73

Categorical Data Analysis Ordinal Outcomes | 1

Overview

- 1. What does ordinal mean? What is an ordinal regression model?
- 2. Derive ORM as a latent variable model
- 3. Apply methods of interpretation from the BRM and MNLM.
- 4. Explore restrictions of the ORM
 - o The parallel regression/proportional odds assumption
 - o Comparing OLM and MNLM
- 5. Alternative models for ordinal outcomes.

Categorical Data Analysis Ordinal Outcomes | 2

What does ordinal mean?

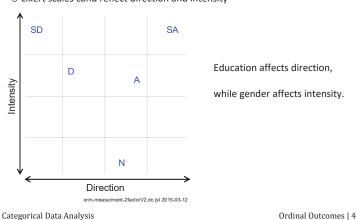


- 1. Are attitudes toward the following statement ordinal?
 - A working mother can establish just as warm and secure of a relationship with her child as a mother who does not work.
- 2. An ordinal variable is ordered on a $\underline{\text{single}}$ dimension with unknown distances between categories
- 3. If values can be ordered does not mean they should be ordered

Categorical Data Analysis Ordinal Outcomes | 3

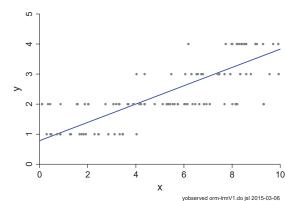
Variables can be ordered on multiple dimensions

- o Occupations can be ordered on both status and income
- o Likert scales cand reflect direction and intensity



Ordinal is not interval

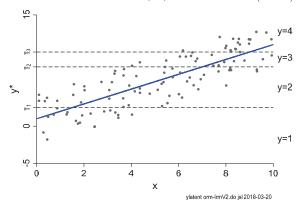
Treating an ordinal variable as interval can produce misleading results.



Categorical Data Analysis Ordinal Outcomes | 5

A latent variable model for ordinal outcomes

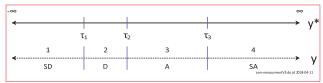
Assume $y^* = \mathbf{x}\boldsymbol{\beta} + \varepsilon$ where $\varepsilon \sim N\left(0,1\right)$ for probit and $\varepsilon \sim \lambda\left(0,\pi^2/3\right)$ for logit



Categorical Data Analysis Ordinal Outcomes | 6

The measurement model

A working mother can establish just as warm and secure of a relationship with her child as a mother who does not work.



1. The propensity y^* and the observed responses are linked by:

$$y_{i} = \begin{cases} 1 \Rightarrow \text{SD-Strongly Disagree} & \text{if} \quad \tau_{0} = -\infty \leq y_{i}^{*} < \tau_{1} \\ 2 \Rightarrow \text{D-Disagree} & \text{if} \quad \tau_{1} \leq y_{i}^{*} < \tau_{2} \\ 3 \Rightarrow \text{A-Agree} & \text{if} \quad \tau_{2} \leq y_{i}^{*} < \tau_{3} \\ 4 \Rightarrow \text{SA-Strongly Agree} & \text{if} \quad \tau_{3} \leq y_{i}^{*} < \tau_{4} = \infty \end{cases}$$

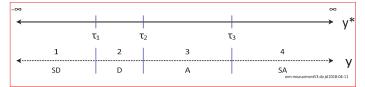
2. In general:

$$y_i = q$$
 if $\tau_{q-1} \le y_i^* < \tau_q$ for $q = 1$ to J

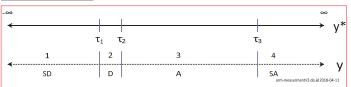
Categorical Data Analysis Ordinal Outcomes | 7

We don't know the thresholds

How can you determine if these are the correct thresholds



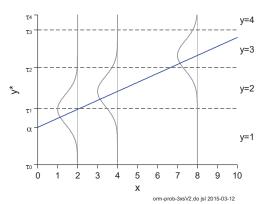
Or these are correct?



Categorical Data Analysis Ordinal Outcomes | 8

Regression linking y to y*

ML fits this model based on observed y and x's



Categorical Data Analysis

ML estimation

1. The probability that the observed outcome q was observed for case i:

$$p_i = \Pr(y_i = q \mid \mathbf{x}_i, \boldsymbol{\beta}, \boldsymbol{\tau}) = F(\tau_q - \mathbf{x}_i \boldsymbol{\beta}) - F(\tau_{q-1} - \mathbf{x}_i \boldsymbol{\beta})$$

2. With independent observations:

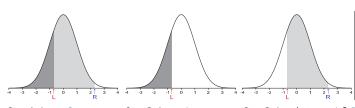
$$L(\boldsymbol{\beta}, \boldsymbol{\tau} \mid \mathbf{y}, \mathbf{X}) = \prod^{N} p_{i}$$

Software issues

- 1. You must know which parameterization is used for identification.
- 2. Different methods of maximization produce *slightly* different test statistics.
- 3. ORM takes longer to converge than some models.
- 4. Small N's in a category can lead to failure to converge.
 - o You can merge adjacent categories and only lose efficiency

Computing $Pr(y=k \mid X)$

 $Pr(y=m \mid x)$ is the area between two thresholds



Step 1. Area ≤ R Step 2. Area ≤ L Step 3. Area between L & R

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Categorical Data Analysis

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Ordinal Outcomes | 9

Computing Pr(y=2|x)

1. If y=2 then y* is between τ_1 and τ_2 .

$$\Pr(y=2 \mid X) = \Pr(\tau_1 \leq y^* < \tau_2 \mid X)$$

2. Expanding y*:

$$\Pr(y=2 \mid X) = \Pr(\tau_1 \leq \alpha + \beta x + \varepsilon < \tau_2 \mid X)$$

3. Isolating ϵ :

$$\Pr(y=2 \mid X) = \Pr(\tau_1 - \alpha - \beta X \le \varepsilon < \tau_2 - \alpha - \beta X \mid X)$$

4. Generalizing, the probability is a difference of CDFs:

$$\Pr(y = m \mid \mathbf{x}) = F(\tau_m - \mathbf{x}\boldsymbol{\beta}) - F(\tau_{m-1} - \mathbf{x}\boldsymbol{\beta})$$

5. $CDF(-\infty) = 0$ and $CDF(\infty) = 1$ for computing the first and last categories.

Categorical Data Analysis

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Identification: you can't estimate all thresholds and intercepts

- 1. Suppose that true parameters are α and the $\tau_m s$.
- 2. Create $\underline{imposter\ parameters}$ by subtracting an unknown δ :

$$\alpha^* = \alpha - \delta$$
 and $\tau_a^* = \tau_a - \delta$

3. Probabilities are unaffected since $\delta - \delta = 0$:

$$\begin{split} \Pr \big(\, \mathbf{y} = q \, | \, \mathbf{x} \, \big) &= F \Big(\tau_q - \alpha - \beta \mathbf{x} + \left[\mathbf{\delta} - \delta \, \right] \Big) - F \Big(\tau_{q-1} - \alpha - \beta \mathbf{x} + \left[\mathbf{\delta} - \delta \, \right] \Big) \\ &= F \Big(\left[\, \tau_q - \delta \, \right] - \left[\, \alpha - \mathbf{\delta} \, \right] - \beta \mathbf{x} \Big) - F \Big(\left[\, \tau_{q-1} - \delta \, \right] - \left[\, \alpha - \delta \, \right] - \beta \mathbf{x} \Big) \\ &= F \Big(\tau_q^* - \boldsymbol{\alpha}^* - \beta \mathbf{x} \Big) - F \Big(\tau_{q-1}^* - \alpha^* - \beta \mathbf{x} \Big) \end{split}$$

4. Identifying assumptions must be made such as:

Alternative 1: $\tau_1 = 0$ forces δ to equal τ_1

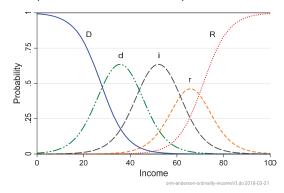
Alternative 2: $\alpha = 0$ forces δ to equals α

5. These assumptions lead to different <u>parameterizations</u> that do not affect the βs or their significance or the probabilities.

Categorical Data Analysis Ordinal Outcomes | 13

What is an ordinal regression model? (Anderson 1980)

- 1. Inherent in the model is this pattern of between regressors and outcomes.
- 2. Your predictions must conform to this pattern



Categorical Data Analysis Ordinal Outcomes | 14

Example: Attitudes toward working mothers

A working mother can establish just as warm and secure a relationship with her child as a mother who does not work.

o Agreeing supports working women

	Freq.	Percent
1 Strong Disagree	297	12.95
2 Disagree	723	31.53
3 Agree	856	37.33
4 Strong Agree	417	18.19
Total	2,293	100.00

Variable	Mean	Min	Max	Label
yr89	.3986044	0	1	Survey year: 1=1989 0=1977
male	.4648932	0	1	Gender: 1=male 0=female
white	.8765809	0	1	Race: 1=white 0=not white
age	44.93546	18	89	Age in years
ed	12.21805	0	20	Years of education
prst	39.58526	12	82	Occupational prestige

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Ordinal logit

. ologit warm i.yr89 i.male i.white age ed prst

Ordered logistic regression

Number of obs = 2293 LR chi2(6) = 301.72 Prob > chi2 = 0.0000 Pseudo R2 = 0.0504

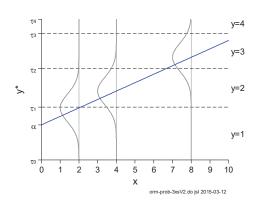
Log likelihood	1 = -2844.912	3		Prob	> CH12 =	0.0504
warm	Coef.	Std. Err.	z	P> z	[95% Conf.	Interval]
yr89 1989 male	.5239025	.0798989	6.56	0.000	.3673036	.6805014
Male white	7332997	.0784827	-9.34	0.000	887123	5794765
White	3911595	.1183808	-3.30	0.001	6231816	1591373
age	0216655	.0024683	-8.78	0.000	0265032	0168278
ed	.0671728	.015975	4.20	0.000	.0358624	.0984831
prst	.0060727	.0032929	1.84	0.065	0003813	.0125267
/cut1	-2.465362	.2389128			-2.933622	-1.997102
/cut2	630904	.2333156			-1.088194	1736138
/cut3	1.261854	.234018			.8031871	1.720521

. estimates store olm $\ensuremath{//}$ to restore estimates after margins, post

Categorical Data Analysis Ordinal Outcomes | 16

Predicted probabilities

$$\Pr(y = q \mid \mathbf{x}) = F(\hat{\tau}_q - \mathbf{x}\hat{\boldsymbol{\beta}}) - F(\hat{\tau}_{q-1} - \mathbf{x}\hat{\boldsymbol{\beta}})$$



Categorical Data Analysis

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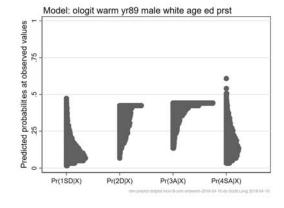
Using predictions for interpretation

- 1. Predictions at observed values
- 2. Marginal effects
- 3. Ideal types
- 4. Tables of probabilities
- 5. Plots of probabilities

Categorical Data Analysis Ordinal Outcomes | 18



I start by examining the distribution of predictions.



Categorical Data Analysis Ordinal Outcomes | 19

Code for predictions at observed values

Make predictions

- 1. One prediction for each level of the outcome:
- . predict OLMpr1sd OLMpr2d OLMpr3a OLMpr4sa
- 2. Add labels
- . label var OLMpr1sd "Pr(1SD | X)"
- . label var OLMpr2d "Pr(2D|X)"
 . label var OLMpr3a "Pr(3A|X)"
- . label var OLMpr4sa "Pr(4SA|X)"

Examine predictions

- 1. Summary statistics
- . sum OLMpr1sd OLMpr2d OLMpr3a OLMpr4sa

Variable	Obs	Mean	Std. Dev.	Min	Max
OLMpr1sd	2293	.1291898	.0827858	.0078648	.4583639
OLMpr2d	2293	.3152269	.0702155	.0811076	.4066651
OLMpr3a	2293	.3740882	.0585058	.1494467	.4274917
OLMpr4sa	2293	.1814951	.0976008	.018211	.5864362

- 2. Histogram
- dotplot OLMpr1 OLMpr2 OLMpr3 OLMpr4, ylab(0(.25)1, grid gmin gmax) ///
 title(Model: ologit warm yr89 male white age ed prst, position(11)) ///
 ytitle(Predicted probabilities at observed values)
- 3. Export to PNG since EMF can be very large

graph export `pgm'-`graphname'.png, width(1600) replace

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Categorical Data Analysis Ordinal Outcomes | 21

Tables of predicted probabilities: gender and age

- 1. When you have important categorical regressors, tables are effective.
- Where should you hold the other variables?
 Global means are simpler but can be misleading
 Local means are harder but sometimes more realistic
- ${\bf 3.\,A\,sensitivity\,analysis\,assesses\,how\,important\,this\,decision\,is.}$

Gender and year with global means: agree supports working women

- 1. Theory, past research, and the regression coefficients suggests:
- o Men are more negative than women
- \circ Attitudes are more positive in 1989 than 1977

A. 1977	SD	D	A	SA	
Men	0.19	0.40	0.32	0.10	
Women	0.10	0.31	0.41	0.18	
Men-Women	0.09	0.09	-0.09	-0.08	DCR(male 1977)
B. 1989	SD	D	Α	SA	
Men	0.12	0.34	0.39	0.15	
Women	0.06	0.23	0.44	0.27	
Men-Women	0.06	0.11	-0.05	-0.12	DCR(male 1989)
C. 1977 to 1989	SD	D	Α	SA	
Men	-0.07	-0.06	0.07	0.05	DCR(yr89 male)
Women	-0.04	-0.08	0.03	0.09	DCR(yr89 female)

Note: Other variables are held at their means.

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Interpretation

TODO

XYZ

Are global means reasonable

- 1. The predictions are made holding all other variables at their means.
 - o Predictions for men in 1989 hold variables at the same values as predictions for women in 1977
- 2. Is this substantively reasonable?
- 3. What if we make predictions using local means

Pr(y| gender, years, Mean(x|gender, year))

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Predictions with local means: Agree supports working mothers

A. 1977	SD	D	Α	SA
Men	0.19	0.40	0.31	0.09
Women	0.10	0.32	0.41	0.17
Men-Women	0.09	0.09	-0.10	-0.08
B. 1989	SD	D	Α	SA
Men	0.11	0.33	0.40	0.16
Women	0.06	0.23	0.44	0.27
Men-Women	0.05	0.10	-0.04	-0.11
C. 1977 to 1989	SD	D	Α	SA
Men	-0.08	-0.07	0.09	0.07
Women	-0.04	-0.09	0.03	0.10

Note: Other variable are held at means for given year and gender.

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Comparing predictions with global and local means

	1SD	2D	3A	4SA
1977				
Men	-0.00	-0.00	0.00	0.00
Women	-0.00	-0.01	0.00	0.01
1989				
Men	0.01	0.01	-0.01	-0.01
Women	0.00	0.00	-0.00	-0.00
1977	 			
Men_Women	0.00	0.01	-0.00	-0.01
1989	 			
Men_Women	0.01	0.01	-0.01	-0.01

- 1. The differences are substantively small so I am confident that conclusions are not affected by levels of the controls.
- 2. Which set of probabilities would you use? Why?

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Code for tables of predictions

mtable with global means: Agree indicates support

- 1. Atspec at(yr89=(0 1) male=(0 1)) computes predictions for all combinations of yr89 and male
- 2. atmeans holds other variable at global means
- . mtable, at(yr89=(0 1) male=(0 1)) atmeans clear

Expression: Pr(warm), predict(outcome())

	yr89	male	1_SD	2_D	3_A	4_SA
 1	0	0	0.099	0.308	0.413	0.180
2	0	1	0.186	0.403	0.316	0.095
3	1	0	0.061	0.228	0.441	0.270
4	1	1	0.119	0.339	0.390	0.151

Specified values of covariates

I	1.			
į	white	age	ed	prst
Current	. 877	44.9	12.2	39.6

Categorical Data Analysis Ordinal Outcomes | 27

- 3. Since i.male is a regressor, dydx(male) computes DC for gender.
- 4. Option atvars (1.yr89) adds yr89 to the table.
- . mtable, dydx(male) at(yr89=(0 1)) atvars(1.yr89) atmeans

Expression: Marginal effect of Pr(warm), predict(outcome())

	1. yr89	1 SD	2 D	3 A	4 SA
1	0	0.087	0.094	-0.097	-0.085
2	1 1	0.058	0.111	-0.050	-0.119

Specified values of covariates

	1.				
	male	white	age	ed	prst
Current	.465	.877	44.9	12.2	39.6

- 5. To verify my work,
- mchange male, at(yr89=0) atmeans brief // DCmale 1977
- . mchange male, at(yr89=1) atmeans brief // DCmale 1989

Advanced code: Building a nicer table

mtable, at(yr89=0 male=1) atmeans rowname(Men) clear roweqnm(1977) mtable, at(yr89=0 male=0) atmeans rowname(Women) below roweqnm(1977) mtable, dydx(male) at(yr89=0) atmeans rowname(Men_Women) below roweqnm(1977) mtable, at(yr89=1 male=1) atmeans rowname(Men) below roweqnm(1989) mtable, at(vr89=1 male=0) atmeans rowname(Women) below rowegnm(1989) mtable, dydx(male) at(yr89=1) atmeans rowname(Men_Women) below roweqnm(1989) mtable, dydx(yr89) at(male=1) atmeans rowname(77to89) below roweqnm(Men) mtable, dydx(yr89) at(male=0) atmeans rowname(77to89)

1	1 SD	2 D	3 A	4 SA
1977				
Men	0.186	0.403	0.316	0.095
Women	0.099	0.308	0.413	0.180
Men Women	0.087	0.094	-0.097	-0.085
1989				
Men	0.119	0.339	0.390	0.151
Women	0.061	0.228	0.441	0.270
Men Women	0.058	0.111	-0.050	-0.119
Men				
77to89	-0.067	-0.063	0.074	0.056
Women				
77to89	-0.038	-0.080	0.028	0.090

Expression: Marginal effect of Pr(warm), predict(outcome())

Specified values of covariates ...

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Tables using local means

- 1. Check means by by year and gender
- . sort yr89 male
- . by yr89 male: sum white age ed prst

->	yr89 = 1977, male	= Femal	Le			
	Variable	Obs	Mean	Std. Dev.	Min	Max
	white	718	.8760446	.3297604	0	1
	age	718	45.19638	16.59508	19	88
	ed	718	11.73816	2.813291	3	19
	prst	718	37.38579	13.53379	12	78
->	yr89 = 1977, male	= Male				
::						
->	yr89 = 1989, male	= Femal	Le			
::						
->	yr89 = 1989, male	= Male				
	white	405	.8938272	.3084397	0	1
	age	405	43.66667	16.98412	19	89
	ed	405	13.11358	3.368747	0	20
	prst	405	42.16543	14.999	12	82
	- '					

Categorical Data Analysis Ordinal Outcomes I 30

```
2. Combing if with atmeans makes predictions with local means
mtable if yr89==0 & male==1, atmeans rowname(Men)
    clear roweqnm(1977)
mtable if yr89==0 & male==0, atmeans rowname(Women) ///
    below roweqnm(1977)
mtable if yr89==1 & male==1, atmeans rowname(Men) ///
    below roweqnm(1989)
mtable if yr89==1 & male==0, atmeans rowname(Women) ///
    below roweqnm(1989)
```

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Marginal effects: Discrete changes

DC at representative values (DCR and DCM)

1. Discrete change at x* is defined as:

$$\frac{\Delta \Pr\left(y = q \mid \mathbf{x}^*\right)}{\Delta x_k} = \Pr\left(y = q \mid \mathbf{x}^*, \underbrace{\mathsf{End}}_{x_k}\right) - \Pr\left(y = q \mid \mathbf{x}^*, \mathsf{Start}_{x_k}\right)$$

2. Interpretation:

When x_k changes from the start to end, the probability of q changes by MER, holding other variables at \mathbf{x}^* .

3. For example,

Being male decreases the probability of strong support for working mothers by .10, holding other variables at their means.

- 4. The DCR depends on
- o The regression parameters
- \circ The value at which x_k starts and how much it changes
- o Levels of variables that are not changing

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Average DC (AME)

1. Average discrete change:

$$ADC = \frac{1}{N} \sum_{i=1}^{N} \frac{\Delta \Pr(y = q \mid \mathbf{x}_i)}{\Delta x_{ik}},$$

2. Interpretation

On average a change of Δx_k in x_k changes the probability of q by ADC.

3. For example,

On average being male decreases the probability of strongly agreeing that working mothers can be good mothers by .10.

- 4. The ADC depends on
- o The regression parameters
- o The distribution of all regressors

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ADC for all variables

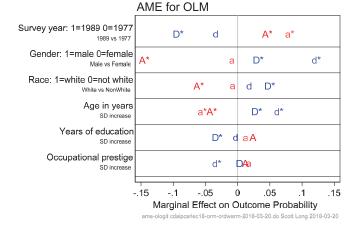
Computing the effects is easy, but there is a lot of information to digest

. mchange, amount(one sd) // see graph that follows ologit: Changes in Pr(y) | Number of obs = 2293

<pre>Expression: Pr(warm), predict(outcome())</pre>								
	1 SD	2 D	3 A	4 SA				
yr89 1989 vs 1977	-0.053	-0.064	0.042	0.075				
p-value	0.000	0.000	0.000	0.000				
male								
Male vs Female	0.079	0.087	-0.066	-0.100				
p-value	0.000	0.000	0.000	0.000				
white								
White vs NonWhite	0.038	0.048	-0.026	-0.059				
p-value	0.000	0.001	0.000	0.002				
age								
+1	0.002	0.003	-0.002	-0.003				
p-value	0.000	0.000	0.000	0.000				
+SD	0.043	0.038	-0.036	-0.046				
p-value	0.000	0.000	0.000	0.000				
ed								
+1	-0.007	-0.008	0.005	0.010				
p-value	0.000	0.000	0.000	0.000				
+SD	-0.021	-0.026	0.015	0.031				
p-value	0.000	0.000	0.000	0.000				
::								

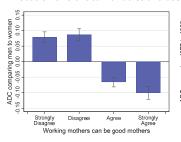
Categorical Data Analysis Ordinal Outcomes | 34

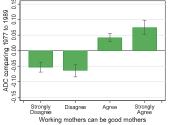
Graph to summarize effects (* indicates significant at .05 level)



Focusing on survey year and gender

1. I focus on two critical variables and use error bars to indicate precision





TODO add summary of findings

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Comparing discrete changes

1. Did the effects of gender change significantly between 1977 and 1989? That is:

Ho: $ADC(gender | 1977, \mathbf{x}^*) = ADC(gender | 1989, \mathbf{x}^*)$

	1 SD	2 D	3 A	4 SA
ADC(male 77)	0.089	0.081	-0.083	-0.088
p-value		0.000	0.000	0.000
ADC(male 89)	0.062	0.099	-0.041	-0.119
p-value	0.000	0.000	0.000	0.000
ΔADC(male)/Δyear p-value	-0.028	0.018	0.042	-0.032
	0.000	0.000	0.000	0.000

The effects of gender changed significantly from 1977 to 1989. From 1977 to 1989 the effect of being male on strongly opposing working women as mothers got 3 points smaller, which was offset by a 2 point increase in opposing working women. Men still were less likely to agree with working women, but the effect was 4 points smaller. But, they were 3 points less to strongly endorse working women as mothers.

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Computing marginal effects

Plotting DCs

Plotting mchange results with mchangeplot

```
mchange, amount(one sd)
```

```
mchangeplot, min(-.15) max(.15) gap(.05) varlabels ///
    mcol(blue blue*.7 red*.7 red) ///
     symbols(D d a A) sig(.05) ///
     title(AME for OLM, position(11)) ///
     aspect(.8) leftmargin(.5)
```

Plotting DCs with marginsplot

margins, dydx(male)

```
marginsplot, recast(bar) ciopts(color(gs5)) ///
    xlab(0.5 " " 1 `""Strongly" "Disagree""' ///
    2 "Disagree" 3 "Agree" ///
    4 `""Strongly" "Agree""! 4.5 " ") ///
    ylab(-.15(.05).15, format(%4.2f)) ///
       yline(0) plotopts(barw(0.7) color(blue*.8)) ///
       xtitle("Working mothers can be good mothers") ///
       ytitle("ADC comparing men to women") title("") ///
       scale(1.2)
```

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Comparing discrete changes

Compute DC(male I year) with mtable

- . qui mtable, dydx(male) at(yr89=0) rowname(DCmale_77) clear
- . mtable, dydx(male) at(yr89=1) rowname(DCmale_89) below

		1 SD	2	D	3 A	4	SA
		·					
DCmale	77	0.089	0.08	1	-0.083 -	0.0	880
DCmale	89	0.062	0.09	9	-0.041 -	0.	119

Using margins since we need to post predictions

- . margins, at(yr89=(0 1) male=(0 1)) post 1._predict : Pr(warm==1), predict(pr outcome(1))
- 4. predict : Pr(warm==4), predict(pr outcome(4))
- : yr89 1. at 4. at : yr89

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```
P> | z |
                 Margin Std. Err.
                                                   Annotated
_predict#_at
                .1085645
                          .0077007
                                     14.10
                                            0.000 <= out 1: 77 women
       1 2
                .1980111
                         .0116351
       4 4
               .1623563 .0111352
                                   14.58 0.000 <= out 4: 89 men
```

<u>lincom to estimate second difference</u>

- -(_b[1bn._predict#3._at]-_b[1bn._predict#4._at])
- (1) 1bn._predict#1bn._at 1bn._predict#2._at 1bn._predict#3._at +
- 1bn._predict#4._at = 0 Coef. Std. Err. P> | z | [95% Conf. Interval]

(1) | -.027685 .0049492 -5.59 0.000 -.0373854 -.0179847

mlincom is easier

. mlincom (1-2)-(3-4)

	lincom	pvalue	11	ul
 +				
1	-0.028	0.000	-0.037	-0.018

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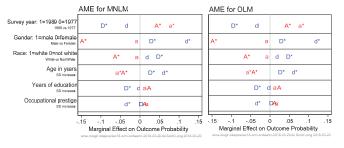
mlincom to create table of differences in effect of gender by year

- . qui mlincom (1-2)-(3-4), rowname(SD) stats(est p) clear qui mlincom (5-6)-(7-8), rowname(D) stats(est p) add qui mlincom (9-10)-(11-12), rowname(A) stats(est p) add mlincom (13-14)-(15-16), rowname(SA) stats(est p) add
- lincom pvalue sp | -0.028 0.000 D 0.018 0.000 0.000 0.042 А -0.032 0.000

The effects of gender on all outcomes changed significantly between 1977 to 1989

Comparing DCs for OLM and MNLM

- 1. Ordinal models require a specific relationship between regressors and predicted probabilities that follow from the assumption that the outcome is ordered on one dimension.
- 2. One way to explore if this assumption is reasonable, is to compare results to multinomial logit.
- 3. Later we will test differences formally



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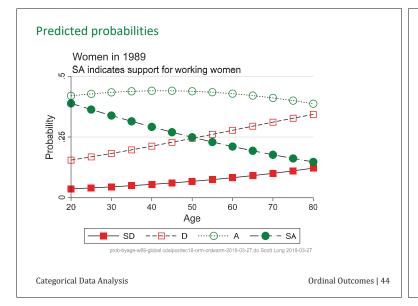
Plotting probabilities

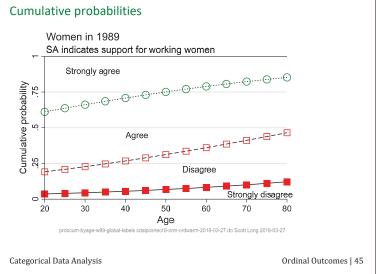
- 1. Plots are more complicated than for the BRM since:
 - o With two outcomes, you plot one probability
 - o With three outcomes, you plot three probabilities
- 2. For ORM and MNLM we can plot probabilities and cumulative probabilities:

Probability: $Pr(y = q | z, X^*)$ as z changes Cumulative probability: $Pr(y \le q | z, X^*)$ as z changes

- 3. These are computed holding other variables constant while changing one.
 - o Excepted for linked variables like x and x2 change together

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Code for plots

Compute predictions with mgen

. mgen, at(age=(20(5)80) male=0 yr89=1) atmeans stub(W89)

Variable	Obs Ur	nique	Mean	Min	Max	Label
W89pr1	13	13	.0720984	.0364676	.121933	pr(y=1 SD) from margins
W89111	13	13	.0586271	.0384676	.097223	95% lower limit
W89ul1	13	13	.0855696	.044771	.146643	95% upper limit
W89age	13	13	50	20	80	Age in years
W89Cpr1	13	13	.0720984	.0364676	.121933	pr(y<=1_SD)
W89pr2	13	13	.2465	.1551205	.3431755	pr(y=2_D) from margins
::						

Specified values of covariates

yr89	male	white	ed	prst
label var W89 label var W89 label var W89 label var W89	pr2 "D"	.8765809	12.21805	39.58526

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```
Globals with characteristics for symbols
global warmsym "mcol(red red*.9 green*.9 green) "
global warmsym "$warmsym msym(s sh Oh O) msiz(3.5 3.5 3 3)" // symbol details
Plot predicted probabilities
graph twoway connected W89pr1 W89pr2 W89pr3 W89pr4 W89age, $warmsym ///
     title(Women in 1989, pos(11)) ///
subtitle("SA indicates support for working women", pos(11)) ///
     xtitle("Age") xlab(20(10)80) ///
ytitle("Probability") ylab(0(.25).50, grid gmin gmax) ///
plotregion(margin(zero) lcol(white)) legend(rows(1)) scale(*1.1)
```

Plot cumulative probabilities with interior text labels graph twoway connected W89Cpr1 W89Cpr2 W89Cpr3 W89age, \$warmsym ///

ph twoway connected W89Cpr1 W89Cpr2 W89Cpr2 W89Cpr3 W89age, \$warmsym ///
title(Women in 1989, pos(11)) \$warmsym ///
subtitle("SA indicates support for working women", pos(11)) ///
xtitle("Age") xlah(20(10)80) yline(1, lcol(black) lwid(*.7)) ///
ytitle("Cumulative probability") ylah(0(.25)1, grid gmin gmax) ///
text(.035 65 "Strongly disagree", place(e)) ///
text(.21 54 "Disagree", place(e)) ///
text(.45 40 "Agree", place(e)) ///
text(.45 40 "Agree", place(e)) ///
text(.90 25 "Strongly agree", place(e)) legend(off) ///
plotregion(margin(zero) lcol(white)) scale(*1.1)

The parallel regression assumption

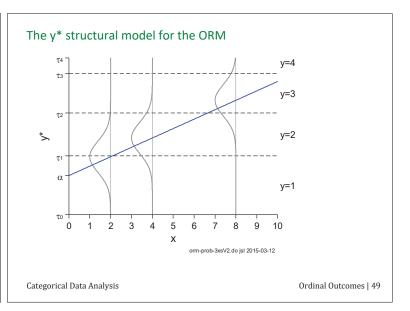
ORM can be thought of as constrained binary regressions

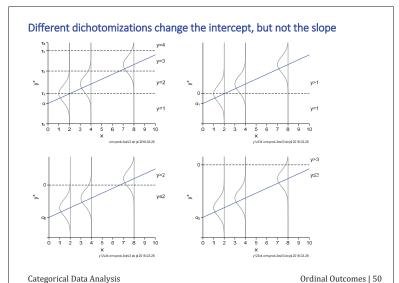
- 1. The outcome y has J categories.
- 2. J-1 binary variables are created:
 - o yj = 1 if y≤j, else 0.
- 3. J-1 binary logits or probits are run on y1, y2, ...
- 4. Slopes are constrained to be equal in all regressions.
- 5. The intercepts are allowed to differ.

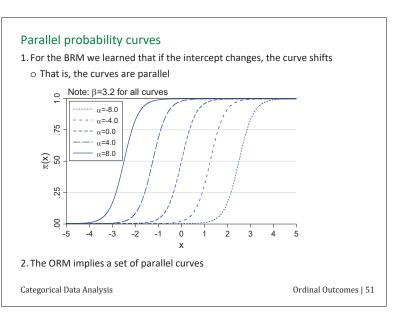
Proportional odds assumption

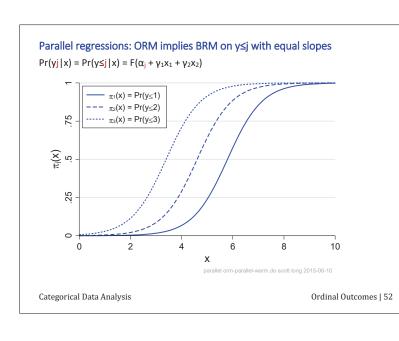
This property is called the proportional odds assumption since the ORs are the same in each $\ensuremath{\mathsf{BRM}}$

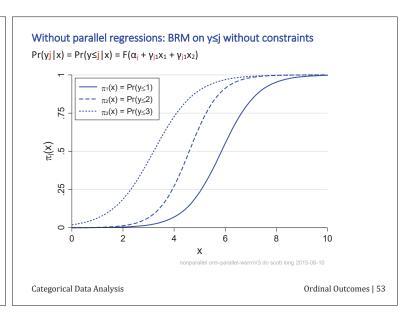
Categorical Data Analysis







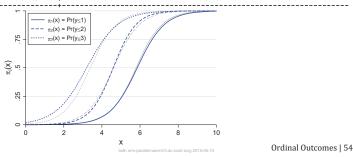




Informal assessment of parallel regressions

1. Informally compare slopes from J-1 binary regressions to those from ORM.

Variable	lt2	1t3	1t4	ologit
Odds ratios				
yr89	0.381***	0.568***	0.727**	1.689***
male	1.357*	1.995***	2.956***	0.480***
white	1.738*	1.369*	1.481*	0.676***
age	1.017***	1.026***	1.019***	0.979***
ed	0.901***	0.949**	0.944*	1.069***
prst	1.001	0.991*	0.994	1.006



Formal tests of parallel regressions

- 1. The Brant test formally compares the coefficients from BLM and ORM
- 2. LR tests can compare gologit2 estimates with ologit estimates
- 3. Tests often reject the parallel regression assumption
- o Rejection might indicate a violation of the parallel regression assumption
- o Rejection could be caused by other violations of the model assumptions
- o The tests might be sensitive to sample size, small categories, or other factors. That is, they might not have good properties
- 4. I rely more on compare the results from an ordinal model to a model that is not ordinal, such as MNLM or GOLM.

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Brant test of parallel regressions

Brant Test of Parallel Regression Assumption

Variable	chi2	p>chi2	df	
All	49.18	0.000	12	
yr89 male white age ed prst	13.01 22.24 1.27 7.38 4.31 4.33	0.001 0.000 0.531 0.025 0.116 0.115		<= these are key variables <= so I need to check them

A significant test statistic provides evidence that the parallel regression assumption has been violated.

LR test of parallel regressions

- gologit2 warm yr89 male white age ed prst, nolog
- est store gologit2
 lrtest ologit gologit2, force // force since not estimated with same command

Likelihood-ratio test (Assumption: ologit nested in gologit2) Prob > chi2 = 0.0000

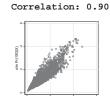
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Comparing ologit and mlogit predictions

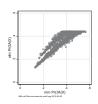
- 1. Before accepting or rejecting the OLM based on a test of parallel regressions, examine whether predictions from the OLM differ from those in a model that does not impose ordinality.
- 2. I typically compare OLM to MNLM. You could also compare to the generalized ordered logit model.
- 3. In general, the results are similar.
 - o Whether differences are substantively important depend on your research goals and require more careful evaluation.

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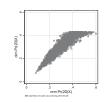
Comparing in sample predictions



Correlation: 0.86



Correlation: 0.92



Correlation: 0.95



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Code for examining parallel regressions assumption

Comparing coefficients from binary logits

ologit warm i.yr89 i.male i.white age ed prst gen warmlt2 = warm<=1 & !missing(warm)</pre> logit warmlt2 i.yr89 i.male i.white age ed prst
gen warmlt3 = warm<=2 & !missing(warm)</pre> logit warmlt3 i.yr89 i.male i.white age ed prst gen warmlt4 = warm<=3 & !missing(warm) logit warm1t4 i.yr89 i.male i.white age ed prst

Brant test of parallel regressions

brant, detail

LR test of parallel regressions

ologit warm yr89 male white age ed prst est store ologitmodel gologit2 warm yr89 male white age ed prst, nolog est store gologit2model
* force since compare models from different estimation commands

1rtest ologit gologit2, force

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Comparing in sample predictions

ologit warm i.yr89 i.male i.white age ed prst predict OLMpr1 OLMpr2 OLMpr3 OLMpr4 mlogit warm i.yr89 i.male i.white age ed prst predict NRMpr1 NRMpr2 NRMpr3 NRMpr4 pwcorr OLMpr1 NRMpr1

pwcorr OLMpr2 NRMpr2 pwcorr OLMpr3 NRMpr3 pwcorr OLMpr4 NRMpr4

Plot predictions

scatter OLMpr1 NRMpr1

Compare other predictions

- 1. Compare plots from mgen
- 2. Compare DCs from mchange

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Modeling political party

This example from the American National Election Study taught me to <u>never</u> assume an outcome is ordinal.

Party ID	Freq.	Percent	Cum.
StrDem	266	19.25	19.25
Dem	427	30.90	50.14
Indep	151	10.93	61.07
Rep	369	26.70	87.77
StrRep	169	12.23	100.00
Total	1 382	100 00	

1382

·					
Variable	Obs	Mean	Std. Dev.	Min	Max
party	1382	2.817656	1.342787	1	5
age	1382	45.94645	16.78311	18	91
income	1382	37.45767	27.78148	1.5	131.25
black	1382	.1374819	.34448	0	1
female	1382	.4934877	.5001386	0	1
educ	İ				
hs only	1382	.5803184	.4936854	0	1

.2590449

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.4382689

OLM

. ologit party age10 income10 i.black i.female i.educ

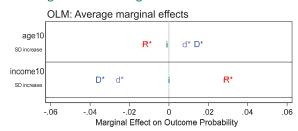
Ordered logistic regression 1,382 Number of obs T.R chi2(6) 212.68 Prob > chi2 Log likelihood = -2010.1976 Pseudo R2 0.0502 party | Coef. Std. Err. P > |z|[95% Conf. Interval] -.0635915 .0312192 -.12478 -.002403 -2.04 0.042 .0961097 .0200567

- 1. Substantive research would be concerned with the effects of all regressors.
- 2. For methodological reasons, I will focus on age and income
 - o age10 is years in ten-year units white is signifcant at the .04 level.
 - o income10 is income in \$10,000 units which is significant at the .001 levels.
- 3. Consider the ADC(age) and ADC(income)

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OLM: Average discrete change

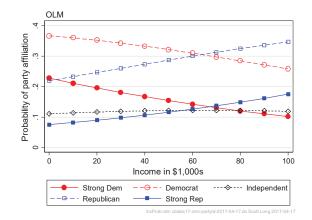
college



- 1. Income significantly decreases the probabilities of both Democratic affiliations and significantly increases the probabilities of both Republican affiliations.
- 2. The effects of age are smaller, with age significantly increases the probabilities of both Democratic affiliations and significantly decreases the probabilities of both Republican affiliations.
- 3. Graphs of predicted probabilities show that since the relationships are nearly linear, the ADCs are good summaries of the effects.

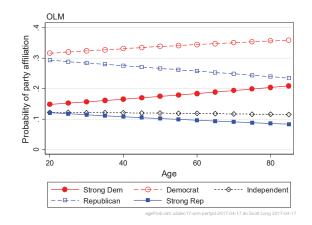
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OLM: Predicted probabilities by income



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OLM: Predicted probabilities by age



Categorical Data Analysis

MNLM model

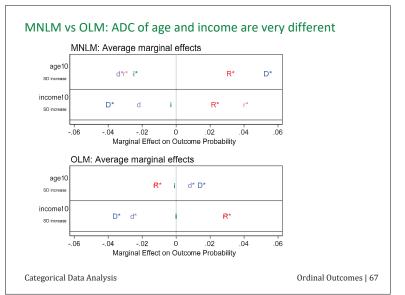
- 1. We fit this model in the lecture on MNLM.
- 2. Both age and income are were significant at the .001 levels: Wald tests for independent variables (N=1382)

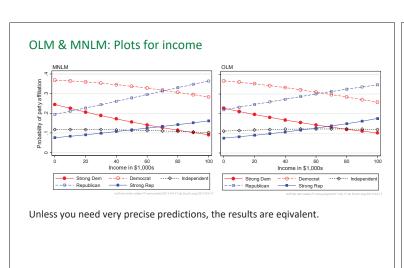
Ho: All coefficients associated with given variable(s) are 0

			P>chi2			
age10	43.815			p=.042	for	OLM
income10	22.985	4	0.000	000.=q	for	OLM

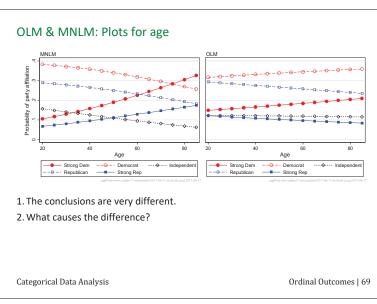
3. Let's compare the ADCs.

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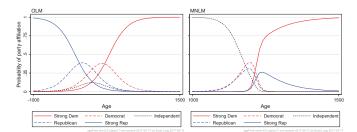




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Extending the range of predictions



- 1. Ordinal models must have the pattern described by Anderson
 - o This is shown on the left
 - This <u>forces</u> the probabilities of end categories to either always get larger or always get smaller
- 2. Nominal models do not have this constraint on predictions

Categorical Data Analysis Ordinal Outcomes | 70

* Comparing MEs from ologit and mlogit

- 1. To test if results from OLM & MNLM differ, we estimate them simultaneously
- 2. Create two copies of the outcome variable to trick gsem

clonevar partyOLM = party
clonevar partyMNL = party

3. Estimate both models simultaneously:

Categorical Data Analysis

Comparing DCM(age+SD)

	lincom	se	pvalue
StrDem	,		
OLM	0.015	0.008	0.064
MNL	0.054	0.010	0.000
Difference	-0.039***	0.007	0.000
Dem	İ		
OLM	0.012	0.006	0.057
MNL	-0.030	0.014	0.028
Difference	0.042***	0.013	0.001
Indep	İ		
OLM	-0.002	0.001	0.099
MNL	-0.026	0.010	0.010
Difference	0.024**	0.010	0.015
Repub			
OLM	-0.015	0.008	0.063
MNL	-0.026	0.013	0.050
Difference	0.011	0.012	0.348
StrRep			
OLM	-0.010	0.005	0.055
MNL	0.027	0.009	0.002
Difference	-0.037***	0.007	0.000

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Comparing DCM(inc+sd)

I	lincom	se	pvalue
StrDem			
OLM	-0.038	0.008	0.000
MNL	-0.046	0.015	0.002
Difference	0.009	0.013	0.500
Dem			
OLM	-0.029	0.006	0.000
MNL	-0.021	0.016	0.190
Difference	-0.008	0.015	0.619
Indep			
OLM	0.004	0.001	0.001
MNL	-0.003	0.012	0.799
Difference	0.007	0.012	0.554
Repub			
OLM	0.037	0.008	0.000
MNL	0.048	0.013	0.000
Difference	-0.010	0.011	0.363
G+D			
StrRep			
OLM	0.025	0.005	0.000
MNL	0.023	0.008	0.004
Difference	0.002	0.005	0.727

Categorical Data Analysis Ordinal Outcomes | 73

Code

Code to compare DCM's for age

Set up margins command

```
sum age10
local mnage = r(mean)
```

local sdage = r(sd) local start = `mnage'-(`sdage'/2) local end = `mnage'+(`sdage'/2)

Compute predictions

```
. margins, at(age=(`start' `end')) atmeans post
#
1._predict : Predicted mean (1.partyOLM), predict(pr outcome(partyOLM 1))
##
```

10._predict : Predicted mean (5.partyMNL), predict(pr outcome(partyMNL 5)) 1. at : age10 3.75549 income10 3.745767 (mean) 0.black .8625181 (mean) 1.black .1374819 (mean) 1.female .4934877 (mean) .1606368 (mean) .5803184 (mean) 1.educ 2.educ 3.educ .2590449 (mean)

Categorical Data Analysis Ordinal Outcomes | 74

::	Margin	Std. Err.	z	P> z	[95% Conf.	Interval]
_predict#_at						
1 1	.1631553	.0100932	16.16	0.000	.1433729	.1829377
1 2	.1782558	.0118232	15.08	0.000	.1550827	.2014288
2 1	.3292235	.0137389	23.96	0.000	.3022958	.3561512
2 2	.3407948	.0143541	23.74	0.000	.3126612	.3689283
::						
9 1	.2686426	.0163059	16.48	0.000	.2366836	.3006017
9 2	.2425236	.0156883	15.46	0.000	.2117751	.273272
10 1	.0913318	.0111995	8.15	0.000	.0693812	.1132825
10 2	.1187061	.0126255	9.40	0.000	.0939606	.1434516

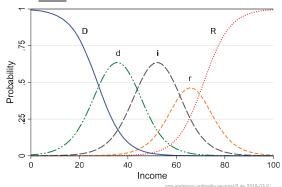
Computing DC's for each model and then second differences

```
qui {
    mlincom 12-1, rowname("StrDem:OLM") stat(est se p) clear
    mlincom (2-1)-(12-11), rowname("StrDem:NNL") stat(est se p) add
    mlincom (2-1)-(12-11), rowname("StrDem:Difference") stat(est se p) add
    mlincom 10-9, rowname("StrRep:OLM") stat(est se p) add
    mlincom 20-19, rowname("StrRep:MNL") stat(est se p) add
    mlincom (10-9)-(20-19), rowname("StrRep:Difference") stat(est se p) add
}
mlincom, stat(est se p) twidth(15) dec(3) ///
    title("DC age for SD Change at Mean Across OLM and MNL")
```

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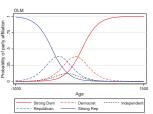
Ordinal or nominal?

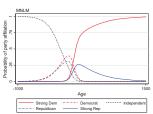
 I find ordinal regression models are often overly restrictive even if the outcome <u>seems</u> to be ordinal.



Categorical Data Analysis Ordinal Outcomes | 76

- 2. Ordinality is relaxed in the MNLM and the generalized ordered logit model
- 3. I prefer MNLM because I find the results more intuitive
- 4. Returning to our example of political party, compare what happens in the OLM and MNLM if we extend the range of age:





5. Any time you are use an ordinal regression model, compare the result to those from a model that is not ordinal.

Overview of ordinal LHS

- 1. If you are using LRM for ordinal outcomes, consider y* standardized coefficients from the ORM (below).
 - o If you must use the LRM, at least verify that the conclusions are consistent with those from the ORM.
- 2. Before using ordinal models, consider whether your variable is ordinal as Stevens defined it.
 - o Categories are ranked on a single dimension
- 3. Always do a sensitivity analysis before accepting the results of ORM.
- o Compare results to those from a nominal model (MNLM or GOLM).
- 4. Even if you don't find the ORM useful for your work, this model is the foundation for the IRT and Rasch models for ordinal indicators.

Categorical Data Analysis

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Other methods of interpretation

- 1. I prefer methods based on predictions and marginal effects
- 2. Two other approaches can be used
 - o Regression coefficients for y*
 - o Odds ratios for the odds of larger values of the response

Ordinal Outcomes I 79 Categorical Data Analysis

Interpretation with marginal change in y*

- 1. If you are plan to use LRM with ordinal outcomes, this is a better solution.
- o Sometimes it gives you similar results, but sometimes they differ.
- 2. In the ORM,

$$y^* = \mathbf{x}\boldsymbol{\beta} + \varepsilon = \beta_0 + \beta_1 x_1 + \dots + \beta_K x_K + \varepsilon$$

- 3. The scale of y^* is not identified, so use <u>fully standardized</u> or $\underline{y^*}$ -standardized coefficients.
- 4. To estimate $Var(\hat{y}^*)$

$$Var(\hat{y}^*) = Var(\hat{\beta}x + e) = Var(\hat{\beta}x) + Var(e) + 2Cov(\hat{\beta}x, e)$$
$$= \hat{\beta}^2 Var(x) + Var(e) + 0 \quad \text{where } Var(e) \text{ is assumed.}$$

5. Generalizing:

$$\hat{\sigma}_{v^*}^2 = \hat{\beta}' \operatorname{Var}(\mathbf{x}) \hat{\beta} + \operatorname{Var}(\varepsilon)$$

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6. The y* standardized coefficient

$$\beta_k^{Sy^*} = \frac{\beta_k}{\sigma_y}$$

For a unit increase in x_k , y^* is expected to increase by $\beta_k^{Sy^*}$ standard deviations holding other variables constant.

7. The fully standardized coefficient is:

$$\beta_k^S = \frac{\sigma_k \beta_k}{\sigma_{y^*}} = \sigma_k \beta_k^{Sy^*}$$

For a standard deviation increase in x_k , y^* is expected to increase by β_{ν}^{S} standard deviations, holding other variables constant.

Categorical Data Analysis Ordinal Outcomes | 81

y* standardized coefficients

- ologit warm i.yr89 i.male i.white age ed prst listcoef, help std

ologit (N=2293): Unstandardized and standardized estimates

Observed SD: 0.9282 Latent SD: 1.9411

	b	z	P> z	bStdX	bStdY	bStdXY	SDofX
yr89	0.5239	6.557	0.000	0.257	0.270	0.132	0.490
male	-0.7333	-9.343	0.000	-0.366	-0.378	-0.188	0.499
white	-0.3912	-3.304	0.001	-0.129	-0.202	-0.066	0.329
age	-0.0217	-8.778	0.000	-0.364	-0.011	-0.187	16.779
ed	0.0672	4.205	0.000	0.212	0.035	0.109	3.161
prst	0.0061	1.844	0.065	0.088	0.003	0.045	14.492

b = raw coefficient

z = z-score for test of b=0
P>|z| = p-value for z-test
bStdX = x-standardized coefficient bStdY = v-standardized coefficient

bStdXY = fully standardized coefficient
SDofX = standard deviation of X. listcoef, help std

Interpretations follow...

Categorical Data Analysis Ordinal Outcomes | 82

Examples

P> | z | bStdX bStdY bStdXY SDofX 1.yr89 | 0.52390 6.557 0.000 0.2566 <mark>0.2699</mark> 0.1322 0.4897

In 1989 support was <u>.27</u> standard deviations higher than in 1977, holding other variables constant.

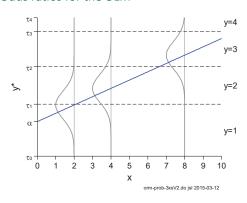
b z P>|z| bStdX bStdY bStdXY SDofX age | -0.02167 -8.778 0.000 -0.3635 -0.0112 -0.1873

Each additional year of age decreases support by .01 standard deviations, holding other variables constant. Alternatively, each additional ten years of age decreases support by .11 standard deviations (=10x-.011), holding other variables constant.

z P>|z| bStdX bStdY bStdXY SDofX ed | 0.06717 4.205 0.000 0.2123 0.0346 0.1094 3.1608

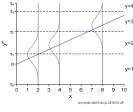
Each standard deviation increase in education increases support by .11 standard deviations, holding other variables constant.

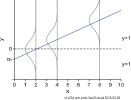
Odds ratios for the OLM

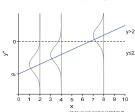


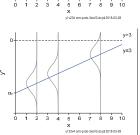
1. $exp(\beta_x)$ is the same for any dichotomization of y.

Categorical Data Analysis Ordinal Outcomes I 84 2. Dichotomizing any place and the slope is unchanged









Ordinal Outcomes I 85 Categorical Data Analysis

3. The cumulative probability equals:

$$\Pr(y \le q \mid \mathbf{x}) = \sum_{i=1}^{q} \Pr(y = j \mid \mathbf{x}) \quad \text{for } q = 1, J - 1$$

4. For S+D+A,

$$\begin{split} \Pr(\mathsf{SD}+\mathsf{D}+\mathsf{A} \mid \mathbf{x}) &= \Pr(\mathbf{y} \leq 3) \\ &= \Pr(\mathbf{y} = 1 \mid \mathbf{x}) + \Pr(\mathbf{y} = 2 \mid \mathbf{x}) + \Pr(\mathbf{y} = 3 \mid \mathbf{x}) \\ &= \left[\Lambda(\tau_1 - \mathbf{x}, \boldsymbol{\beta}) - \Lambda(\tau_0 - \mathbf{x}, \boldsymbol{\beta}) \right] + \left[\Lambda(\tau_2 - \mathbf{x}, \boldsymbol{\beta}) - \Lambda(\tau_1 - \mathbf{x}, \boldsymbol{\beta}) \right] \\ &+ \left[\Lambda(\tau_3 - \mathbf{x}, \boldsymbol{\beta}) - \Lambda(\tau_2 - \mathbf{x}, \boldsymbol{\beta}) \right] \\ &= \left[\Lambda(\tau_3 - \mathbf{x}, \boldsymbol{\beta}) - \Lambda(\tau_0 - \mathbf{x}, \boldsymbol{\beta}) \right] = \Lambda(\tau_3 - \mathbf{x}, \boldsymbol{\beta}) \end{split}$$

5. In general,

$$\Pr(y \le q \mid \mathbf{x}) = \Lambda(\tau_q - \mathbf{x}\boldsymbol{\beta})$$

6. This is a BLM with intercept $\alpha_q = (\tau_q - \beta_0)$ and slopes $\beta^* = -\beta$:

$$\Pr(y \le q \mid \mathbf{x}) = \Lambda(\tau_a - \mathbf{x}\boldsymbol{\beta}) = \Lambda(\alpha_a + \mathbf{x}\boldsymbol{\beta}^*)$$

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7. The odds of $y \le q$ versus y > q given **x** is

$$\Omega_{q}(\mathbf{x}) = \frac{\Pr(y \le q \mid \mathbf{x})}{\Pr(y > q \mid \mathbf{x})} = \exp(\tau_{q} - \mathbf{x}\boldsymbol{\beta}) = \exp(\alpha_{q} + \mathbf{x}\boldsymbol{\beta}^{*})$$

8. The odds ratio for a change in x_k :

$$\frac{\Omega_q(\mathbf{x}, x_k + 1)}{\Omega_q(\mathbf{x}, x_k)} = \exp(\beta_k^*)$$

9. Interpretation

For a unit increase in x_k the odds of lower outcomes compared to higher outcomes change by the factor $\exp(\beta_k^*)$, holding other variables constant.

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Odds ratios for supporting working mothers

NOTE: Odds of higher compared to lower outcome

$$\Omega\!\left(\frac{P(SD)}{P(D,A,SA)}\right) = \Omega\!\left(\frac{P(SD,D)}{P(A,SA)}\right) = \Omega\!\left(\frac{P(SD,D,A)}{P(SA)}\right).$$

ologit (N=2293): Factor change in odds

Odds of: >m vs <=m

oddb ol. >M	VB <-III					
	b	z	P> z	e^b	e^bStdX	SDofX
yr89: 1989	0.5239	6.557	0.000	1.689	1.292	0.490
male: Male	-0.7333	-9.343	0.000	0.480	0.694	0.499
white: White	-0.3912	-3.304	0.001	0.676	0.879	0.329
age	-0.0217	-8.778	0.000	0.979	0.695	16.779
ed	0.0672	4.205	0.000	1.069	1.237	3.161
prst	0.0061	1.844	0.065	1.006	1.092	14.492

b = raw coefficient e^b = exp(b) = factor change in odds for unit increase in X e^bStdX = exp(b*SD of X) = change in odds for SD increase in X SDofX = standard deviation of X

Interpretations on the next page...

Categorical Data Analysis Ordinal Outcomes | 88 Interpretation using odds ratios



From 1977 to 1989, the odds of being more positive toward working women increased by a factor of 1.7, holding other variables constant.

Being male decreases the odds of having more favorable attitudes toward working women by a factor of .48, holding other variables constant.

As standard deviation increase in age, 17 years, decreases the odds of supporting working mothers by a factor of .70, holding other variables constant.

Other ordinal models

The continuation ratio model (ocratio)

- 1. Outcomes are a progression of events or stages in a process
- 2. If $\Pr(y = m \mid \mathbf{x})$ is the probability of being in stage m given \mathbf{x} ,
- 3. The probability of being in stage m or later is

$$\Pr(y \ge m \mid \mathbf{x}) = \sum_{j=m}^{J} \Pr(y = j \mid \mathbf{x})$$

4 The odds

$$\frac{\Pr(y=m \mid \mathbf{x})}{\Pr(y>m \mid \mathbf{x})} = \exp(\tau_m - \mathbf{x}\boldsymbol{\beta})$$

5. Predicted probabilities

$$\Pr\left(y = m \mid \mathbf{x}\right) = \frac{\exp\left(\tau_m - \mathbf{x}\boldsymbol{\beta}\right)}{\prod_{j=1}^{m} \left[1 + \exp\left(\tau_j - \mathbf{x}\boldsymbol{\beta}\right)\right]} \text{ for } m = 1 \text{ to } J - 1$$

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The generalized ordered regression model (glogit2)

- 2. Define

$$\Omega_{y \le q}(\mathbf{x}) = \frac{\Pr(y \le q \mid \mathbf{x})}{\Pr(y > q \mid \mathbf{x})}$$

3. The GOLM removes the restriction of equal \(\beta \) from the OLM:

$$\ln \Omega_{v \leq q}(\mathbf{x}) = \tau_q - \mathbf{x} \boldsymbol{\beta}_q \quad \text{for } q = 1, J - 1$$

4. In terms of odds

$$\Omega_{y \le q}(\mathbf{x}) = \exp(\tau_q - \mathbf{x}\boldsymbol{\beta}_q)$$
 for $q = 1, J - 1$.

5. Predicted probabilities

$$\Pr\left(y = j \mid \mathbf{x}\right) = \frac{\exp\left(\tau_{j} - \mathbf{x}\boldsymbol{\beta}_{j}\right)}{1 + \exp\left(\tau_{j} - \mathbf{x}\boldsymbol{\beta}_{j}\right)} - \frac{\exp\left(\tau_{j-1} - \mathbf{x}\boldsymbol{\beta}_{j-1}\right)}{1 + \exp\left(\tau_{j-1} - \mathbf{x}\boldsymbol{\beta}_{j-1}\right)}$$

6. Software does not enforce that predictions are between 0 and 1.

Categorical Data Analysis

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7. Consider ORs from ologit and gologit2 for political affiliation

Odds of:	OLM	GOLM	Odds of	: MNLM
SD vs D+I+R+SD	0.89**	0.81***	SD vs D	1.25***
SD+D vs I+R+SD	0.89**	0.94*	DvsI	1.07
SD+D+I vs R+SD	0.89**	0.99	I vs R	0.94
SD+D+I+R vs +SD	0.89**	1.14**	R vs SR	0.82***

How do you interpret the OR's for the GOLM? What is your conclusion?

Categorical Data Analysis

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β1a Generalized Marginal Effects

TODO: add more interpretations

Overview

1. The standard definition of a discrete changes is:

$$\frac{\Delta \pi(\mathbf{x})}{\Delta x_k(\text{start} \to \text{end})} = (x_k = \text{end}, \mathbf{x} = \mathbf{x}^*) - \pi(x_k = \text{start}, \mathbf{x} = \mathbf{x}^*)$$

For a change in x_k from start to end, the probability changes by $\Delta \pi/\Delta x_k$, holding other variables at the specified values.

- 2. Sometimes it makes sense to:
 - o Change more than one variable at a time
 - o Make different size changes for different variables
 - $\,\circ\,$ Change a component of an interation variable

Categorical Data Analysis

Generalized Marginal Effects | 1

Review of DC

DCM: change at the center of the data

$$DCM(x_k) = \frac{\Delta \pi(\mathbf{x} = \mathbf{x})}{\Delta x_k (\text{start} \rightarrow \text{end})} = \pi(x_k = \text{end}, \mathbf{x} = \mathbf{x}) - \pi(x_k = \text{start}, \mathbf{x} = \mathbf{x})$$

For someone who is average on all variables, increasing x_k from <u>start</u> to <u>end</u> changes the probability by DCM(x_k)

ADC: average change

$$ADC(x_k) = \frac{1}{N} \sum_{i=1}^{N} \frac{\Delta \pi(\mathbf{x} = \mathbf{x}_i)}{\Delta x_{ik} (\text{start}_i \to \text{end}_i)}$$

On average, increasing x_k from <u>start</u> to <u>end</u> changes the probability by ADC(x_k).

Generalized effects

Here are some extensions to the standard definition of a DC

- 1. Average changes in a subsample
- 2. Proportional change in x_k
- 3. Change in x_k and x_j based on their observed relationship
 - o Change height and what you predict the change in weight to be
- 4. Change of a component in a multiplicative measure
 - o Change weight only as a component of BMI
- 5. Two or more mathematically linked variables
 - o Change age and age-squared

Categorical Data Analysis

Generalized Marginal Effects | 2

Categorical Data Analysis

Generalized Marginal Effects | 3

Example: Health and Retirement Survey

. use hrs-gme-analysis2, clear (hrs-gme-analysis2.dta | Health & Retirement Study GME sample | 2016-04-08)

. codebook diabetes female hsdegree age white bmi weight height, compact

Variable	Obs	Unique	Mean	Min	Max	Label
diabetes	16071	2	.2047166	0	1	Respondent has diabetes?
female	16071	2	.5684774	0	1	Is female?
hsdegree	16071	2	.7624914	0	1	Has high school degree?
age	16071	49	69.29276	53	101	Age
white	16071	2	.7715761	0	1	Is white respondent?
bmi	16071	2469	27.89787	10.57755	82.6728	Body mass index
weight	16071	258	174.9041	73	400	Weight in pounds
height	16071	37	66.28847	48	89	Height in inches

$$\text{Body mass index: } BMI = \frac{weight_{kg}}{height_{m}^{2}} = \frac{703 \times weight_{lb}}{height_{lm}^{2}}$$

Diabetes

Given the diseases burden of diabetes, small changes in Pr(diabetes) are important.

Categorical Data Analysis

Generalized Marginal Effects | 4

Models

1. Two models that vary in how body mass is included

2. Mbmi: uses the BMI index

logit diabetes c.bmi i.white c.age##c.age i.female i.hsdegree estimates store Mbmi

3. Mwt: uses height and weight

logit diabetes c.weight c.height /// i.white c.age##c.age i.female i.hsdegree estimates store Mwt

Categorical Data Analysis

Generalized Marginal Effects | 5

Estimates

Variable	Mbmi	Mwt
bmi	1.1046* 0.000	
weight		1.0165*
height		0.9299*
white White	0.5412*	0.5313*
age c.age#c.age ::	1.3091* 0.9983*	1.3093* 0.9983*
::		
aic bic	14937.47 14991.26	14920.55 14982.03

Note: # significant at .05 level; * at the .001 level.

Categorical Data Analysis

Generalized Marginal Effects | 6

ADC(bmi+sd) and ADC(white)

- . estimates restore Mbmi
- . mchange bmi white

logit: Changes in Pr(y) | Number of obs = 16071

Expression: Pr(diabetes), predict(pr)

	Change	p-value
bmi	 	
+SD	0.097	0.000
white White vs Non-white	-0.099	0.000

Interpretation

Increasing BMI by one standard deviation on average increases the probability of diabetes .097 (p < .001).

On average, the probability of diabetes is .099 less for white respondents than non-white respondents (p < .001).

Categorical Data Analysis

Generalized Marginal Effects | 7

Computing DC with =gen()

margins, at(varnm=gen(exp))

1. To compute predictions at the observed values:

margins, at(bmi = gen(bmi))

2. Predictions at 1 more than the observed value of bmi

margins, at(bmi = gen(bmi + 1))

3. Computing predictions at observed bmi + standard deviation

quietly sum bmi // summary statics local sd = r(sd) // retrieve standard deviation margins, at(bmi = gen(bmi + 'sd'))

4. Computing both average predictions

margins, at(bmi = gen(bmi)) at(bmi = gen(bmi + 1))

ADC(bmi+sd)

1. Compute at observed bmi and observed + sd

Expression : Pr(diabetes), predict()

= bmi+5.770835041238605 : bmi

	!	Delta-method Std. Err.		P> z	[95% Conf.	Interval]
_at 1 2	.2047166 .3017056	.0030338 .005199	67.48 58.03	0.000	.1987704 .2915159	.2106627 .3118954

2. Compute ADC(bmi+sd)

. mlincom 2-1, stats(all)

	lincom	se	pvalue	11	ul
1	 0.097			0.090	0.104

On average, increasing BMI by one standard deviation, about 6 points, increases the probability of diabetes by .097 (p < .001).

Generalized Marginal Effects | 8

Categorical Data Analysis Generalized Marginal Effects | 9

Categorical Data Analysis

Proportional change in xk

- 1. Body mass involves a comparison of height and weight
- 2. Here we include them as separate regressors rather than as BMI

logit diabetes c.weight c.height ///
 i.white c.age##c.age i.female i.hsdegree
estimates store Mwt

- 3. ADC(weight+25) increases weight by 25 pounds
 - : 25 pounds is a 25% increase if you weigh 100 pounds
 - : 25 pounds is an 8% increase if you weigh 300 pounds
- 4. Does increasing weight proportionally make more substantive sense?
- 5. We compute
 - o ADC(weight+25) increasing weight by 25 pounts o ADC(weight*1.14) increasing weight by 14 percent

Categorical Data Analysis

Generalized Marginal Effects | 10

Fixed change in x_k : ADC(weight+25)

- 1. Compute ADC(weight+25)
- . qui estimates restore Mwt
- . mtable, gen(PRadd) ///
- at(weight=gen(weight)) at(weight=gen(weight+25)) post

Expression: Pr(diabetes), predict()

	Pr(y)
	+
1	0.205
2	0.271

. mlincom 2-1

	lincom	-	11	ul
1	0.067	0.000	0.062	0.071

Categorical Data Analysis

Generalized Marginal Effects | 11

Proportional change in x_k : ADC(weight*1.14)

- 1. A simple change computes ADC(weight * 1.14)
- . mtable, gen(PRpct) ///
- > at(weight=gen(weight)) at(weight=gen(weight*1.14)) post

Expression: Pr(diabetes), predict()

	Pr(y)
	+
1	0.205
2	0.273

. mlincom 2-1

	lincom	pvalue	11	ul
1	0 068	0 000	0 063	0 073

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Does ADC(weight*1.14) = ADC(weight+25)?

. qui estimates restore Mwt
. mtable, at(weight=gen(weight)) /// observed
> at(weight=gen(weight+25)) /// + 15

> at(weight=gen(weight*1.14)) post // + 14%
Expression: Pr(diabetes), predict()

	Ţ	Pr(y)	
	1	0.205	
	2	0.271	
	з ј	0.273	
mui	mlincom	(2-1)	

. qui mlincom (2-1), rowname(ADC add) clear qui mlincom (3-1), rowname(ADC pct) add dec(5) mlincom (2-1) - (3-1), rowname(Difference) add dec(5)

		pvalue	11	ul
ADC add	0.06659	0.00000	0.06197	0.07120
ADC pct Difference		0.00000	0.06332	0.07271
Difference	-0.00142	0.00000	-0.00163	-0.00122

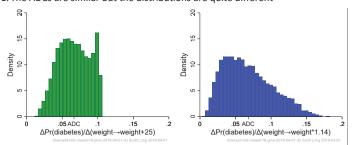
A 14 percent increases in weight has a small but significant larger average effect on diabetes than increasing weight by 25 pounds (p<.001).

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Are they really that similar?

1. The ADCs are similar but the distributions are quite different



2. Does this have implications for health policy?

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Discrete change with linked variables

Mathematically linked variables

1. With polynomials multiple variables must change together

$$\frac{\Delta \pi(\mathbf{x})}{\Delta age(50 \to 60)} = \pi(age=60, agesq=60^2) - \pi(age=50, agesq=50^2)$$

2. Using factor syntax, margins handles this automatically

Substantively linked variables

- 1. Sometimes it makes sense to change multiple variables that are not mathematically linked
- 2. If two people have the same body mass, is the larger person more likely to have diabetes (i.e., taller and proportionally heavier)?
- 3.1 compute an effect where height and weight change proportionally
 - o Use height to predict weight
 - o Use at(...=gen()) to change height and weight together

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Linked variables: ADC(height, weight)

1. Regress weight on height and height-squared (to get a higher R2)

. regress weight c.height##c.height, noci

:: weight	Coef.	Std. Err.	t	P> t
height	-6.338708	1.61073	-3.94	0.000
c.height#c.height	.0855799	.0120867	7.08	0.000
_cons	217.5991	53.5548	4.06	0.000

2. Save the estimates

- . scalar b0 = _b[_cons]
 . scalar b1 = _b[height]
 . scalar b2 = _b[c.height#c.height]
- 3. Predict weight from height

weighthat = b0 + b1*height + b2*height#height

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4. Make predictions:

. qui estimates restore Mwt
. mtable, post commands ///
> at(height=gen(height) weight=gen(weight)) /// observed
/// height + at(height=gen(height+6) /// height + 6 weight=gen(b0 + b1*(height+6) + b2*((height+6)^2))) // => weight

Expression: Pr(diabetes), predict()

	Pr()
1	0.20
2	0.20

. mlincom 2-1

There is no evidence that being physically larger without greater body mass contributes to the incidence of diabetes.

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Decomposing the effect of BMI

1. The BMI index measures relative weight

$$BMI = 703 \times \frac{weight_{lb}}{height_{lm}^2} = 703 \times weight \times height^{-1} \times height^{-1}$$

- 2. With BMI in the model, can we compute the effect of weight change?
 - o Why do this? DC(weight) is clearer to patients than DC(bmi)
- 3. Create components of BMI

generate heightinv = 1/height label var heightinv "1/height" generate factor = 703
label var factor "scale factor to convert from metric"

4. These models are identical

logit diabetes c.factor#c.weight#c.heightinv#c.heightinv /// i.white c.age##c.age i.female i.hsdegree estimates store MbmiFV logit diabetes c.bmi i.white c.age##c.age i.female i.hsdegree estimates store Mbmi

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5. The estimates are identical (so are the standard errors)

Variable	Mbmi	Mbmifv
c.factor# c.weight# c.height_inv# c.height_inv		1.1045533
bmi	1.1045533	
white White	.5411742	.5411742

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- 6. Factor syntax makes it possible to change weight as a component
- . qui estimates restore Mbmifv
- . mchange weight, amount(sd) delta(25)

logit: Changes in Pr(y) | Number of obs = 16071

Expression: Pr(diabetes), predict(pr)

!	Change	p-value
weight		
+delta İ	0.065	0.000

Average predictions

1: Delta equals 25.

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Conclusions on GME

- o Other examples
- o More interpretation

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TODO Conclusions

- 1. LRM, BRM, ORM, MNLM, PRM, NBRM, and ZIP/ZINB are building blocks for models in many areas
- 2. Extensions add panels, hierarchies, clustering, survey sampling, and more
- 3. The basic structure of the models stays the same
- 4. Since the models are nonlinear, the challenge is to determine what is substantively important and to find the best way to summarize the results
- 5. Alternative strategies need to be tried to find the most convincing approach
- 6. Remember Neal Henry's sage advice:

Don't let the numbers get in the way of the data.

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